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WKB MODE SUMMING PROGRAM FOR DIPOLE ANTENNAS OF ARBITRARY ORIEN--ETC(U)
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WKB MODE SUMMING PROGRAM FOR DIPOLE ANTENNAS OF ARBITRARY ORIENTATION AND ELEVATION FOR VLF/LF PROPAGATION

Calculation of vlf/lf field strengths
in the earth-ionosphere waveguide

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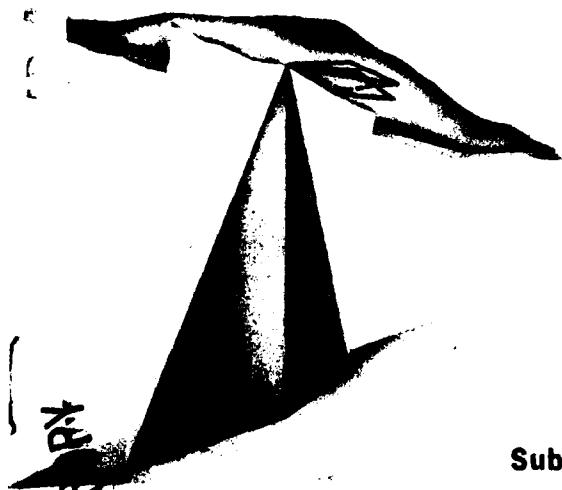
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The computer program described in this report is a modified version of that described in NELC Interim Report 713, NTIS, AD728414. Changes consist of an increase in the number of waveguide slabs from 25 to essentially an unlimited number, more convenient formatting of the input data, especially in the reduction from three to two cards per waveguide mode, an increase in the number of allowable modes from 15 to 30, and the addition of two new output options. This program is referred to as WKBFLDS or FLD4.		

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OBJECTIVE

Develop a computer program for calculating vlf/lf field strengths in the earth-ionosphere waveguide whose characteristics may vary along the direction of propagation.

RESULTS

The computer program described in this report is a modified version of that described in NELC Interim Report 713, WKB Mode Summing Program for VLF/LF Antennas of Arbitrary Length, Shape, and Elevation. Changes consist of an increase in the number of waveguide slabs from 25 to essentially an unlimited number, more convenient formatting of the input data, especially in the reduction from three to two cards per waveguide mode, an increase in the number of allowable modes from 15 to 30, and the addition of two new output options. This program is referred to as WKBFLDS or FLD4.

RECOMMENDATIONS

Use this program in instances where the characteristics of the earth or ionosphere vary slowly along the propagation path.

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INTRODUCTION

Electromagnetic radiation in the lower frequency bands emitted in the region between the finitely conducting earth and the weakly ionized plasma of the lower ionosphere is guided by these boundaries and propagated to great distances around the earth. The waveguide model analyzes this propagation using a mode series (ref 1-4). The propagation parameters of interest (phase velocity, attenuation rate, excitation factor) can be evaluated for each mode. The total field at any point along the guide is then the vector sum of the contributions from each mode. The waveguide model has been employed in a series of computer programs (ref 5-7) useful from vlf to lf.

In many instances, the earth-ionosphere waveguide can be considered to have constant propagation properties along the transmission path. The mode sum calculations made for these cases are referred to as horizontally homogeneous. However, for propagation to great distances it is unrealistic to assume the waveguide parameters will remain constant along the whole length of the path. For example, the direction and strength of the earth's magnetic field will vary along the path, causing changes in the mode parameters due to the anisotropy of the ionosphere. Discontinuities can occur in the lower wall of the waveguide due to the presence of ground conductivity changes. The ionospheric conductivity varies according to the time of day, season, and the presence of the sunrise or sunset line along the propagation path. Anomalous ionization from a nuclear detonation may also produce important changes in mode parameters along the propagation path. If changes in the waveguide parameters are small within a few radio wavelengths, then the modes can be tracked through the region of change.

The computer program described in this report was developed for calculating vlf/lf field strengths in the earth-ionosphere waveguide. Allowance is made for horizontal inhomogeneity in the direction of propagation. The program is based upon a slab model and assumes the waveguide is homogeneous transverse to the great circle path between a transmitter and a receiver. For purposes of identification it is called FLD4 or WKBFLDS.

In the FLD4/WKBFLDS program, field strength calculations can be generated for all electric field components, at any receiver height within the waveguide, generated by electric dipole excitors of arbitrary orientation located

at any height within the guide. Transmitter and receiver heights must be within the free-space portion of the waveguide.

In describing the WKBFLDS computer program, familiarity is assumed with references 5 and 7 which describe FORTRAN programs for obtaining waveguide mode constants within the earth-ionosphere waveguide. Relevant outputs from these programs are the mode eigenangles and four independent quantities from which the excitation factors may be determined. Principal outputs of the WKBFLDS program are listings of the mode sum parameters and the corresponding plots. The field strengths are given in dB above 1 μ V/m and the phase is given relative to free space propagation.

The Summary of the Equations section summarizes the relevant formulae. A description of the program input, output, and operating procedures is given in the Program Execution section. The appendix contains a FORTRAN listing of the computer program.

SUMMARY OF THE EQUATIONS

BACKGROUND

In the propagation of vlf and lf terrestrial radio waves to great distances, the waves are confined within the space between the earth and the ionosphere. This space acts as a waveguide.

The waveguide mode method described in references 6 and 7 obtains the full-wave solution for a waveguide that is characterized by arbitrary electron and ion density distributions and collision frequencies with height and a lower boundary which is a smooth homogeneous earth with an adjustable surface conductivity and dielectric constant. The model allows for earth curvature, ionospheric inhomogeneity, and anisotropy.

The propagation geometry is shown in figure 1. The vertical coordinate is z , the direction of propagation is x , and y is normal to the plane of propagation. Thus, the fields exhibit no y dependence and have a dependence on x of the form $\exp(-ikS_m x)$. All field quantities are assumed to have an $\exp(i\omega t)$ dependence where ω is the angular frequency. The dipole source for the fields is denoted in figure 1 by \vec{M} . The dipole is oriented at an inclination angle γ

measured from the vertical, and azimuthal angle θ measured from the x-axis. For a horizontal dipole $\gamma = 90^\circ$, and $\theta = 0^\circ$ represents end-fire launching.

The energy within the waveguide is considered to be partitioned among a series of modes called the eigenangles (or "modes") and designated by the complex angle, θ , obtained by solving the determinantal equation:

$$F(\theta) = |\tilde{R}(\theta) \tilde{R}(\theta) - 1| = 0 \quad (1)$$

where

$$\tilde{R}(\theta) = \begin{pmatrix} \parallel R_{\parallel}(\theta) & \perp R_{\parallel}(\theta) \\ \parallel R_{\perp}(\theta) & \perp R_{\perp}(\theta) \end{pmatrix} \quad (2)$$

and

$$\tilde{R}(\theta) = \begin{pmatrix} \parallel \bar{R}_{\parallel}(\theta) & 0 \\ 0 & \perp \bar{R}_{\perp}(\theta) \end{pmatrix} \quad (3)$$

are the complex ionospheric reflection coefficient matrices looking up into the ionosphere and down towards the ground, respectively, from a height "d".

Once equation 1 is solved for as many modes, θ_m , as needed, the mode parameters, phase velocity, attenuation rate, and excitation factors can be computed. Let S_m be the sine of the eigenangle θ_m and let the individual components be S_r and S_i so that $S_m = S_r + i S_i$. The phase velocity is given by

$$v = \frac{c}{S_r} \quad (4)$$

where c is the vacuum speed of light.

The attenuation rate is given by

$$\alpha = -8.6859k S_i \quad (\text{in dB/unit distance}) \quad (5)$$

where k is the free-space wave number.

The excitation factor formulae, as given in reference 1, are summarized in table 1. The headings apply to the electric field components (E_z , E_y , E_x) excited by a vertical dipole (z), a horizontal dipole broadside (y), and a horizontal dipole end-on (x).

Field Component	z	y	x
Exciter			
z	$\frac{s^{5/2} (1 + \bar{R}_{\parallel})^2 (1 - \bar{R}_{\perp\perp} R_{\perp})}{F'(\theta_m) \bar{R}_{\parallel} D_{11}}$	$-\frac{s^{3/2} \bar{R}_{\perp} (1 + \bar{R}_{\parallel}) (1 + \bar{R}_{\perp})}{F'(\theta_m) D_{12}}$	$\frac{s^{3/2} (1 + \bar{R}_{\parallel})^2 (1 - \bar{R}_{\perp\perp} R_{\perp})}{F'(\theta_m) \bar{R}_{\parallel} D_{11}}$
y	$-\frac{s^{3/2} \bar{R}_{\perp} (1 + \bar{R}_{\perp}) (1 + \bar{R}_{\parallel})}{F'(\theta_m) D_{12}}$	$\frac{s^{1/2} (1 + \bar{R}_{\perp})^2 (1 - \bar{R}_{\parallel\parallel} R_{\parallel})}{F'(\theta_m) \bar{R}_{\perp} D_{22}}$	$-\frac{s^{1/2} \bar{R}_{\parallel} (1 + \bar{R}_{\perp}) (1 + \bar{R}_{\parallel})}{F'(\theta_m) D_{12}}$
x	$-\frac{s^{3/2} (1 + \bar{R}_{\parallel})^2 (1 - \bar{R}_{\perp\perp} R_{\perp})}{F'(\theta_m) \bar{R}_{\parallel} D_{11}}$	$\frac{s^{1/2} \bar{R}_{\perp} (1 + \bar{R}_{\parallel}) (1 + \bar{R}_{\perp})}{F'(\theta_m) D_{12}}$	$-\frac{s^{1/2} (1 + \bar{R}_{\parallel})^2 (1 - \bar{R}_{\perp\perp} R_{\perp})}{F'(\theta_m) \bar{R}_{\parallel} D_{11}}$

Table 1. Excitation factors

In table 1 the following terms are used:

$$F'(\theta_m) = \left. \frac{\partial F}{\partial \theta} \right|_{\theta=\theta_m} \quad (6)$$

$$F_1 = - \left\{ H_2(q_o) - i \frac{n_o^2}{n_g^2} \left(\frac{ak}{2} \right)^{1/3} (n_g^2 - s^2)^{1/2} h_2(q_o) \right\} \quad (7)$$

$$F_2 = H_1(q_o) - i \frac{n_o^2}{n_g^2} \left(\frac{ak}{2} \right)^{1/3} (n_g^2 - s^2)^{1/2} h_1(q_o) \quad (8)$$

$$F_3 = - \left\{ h_2^*(q_o) - i \left(\frac{ak}{2} \right)^{1/3} (n_g^2 - s^2)^{1/2} h_2(q_o) \right\} \quad (9)$$

$$F_4 = h_1'(q_o) - i \left(\frac{ak}{2}\right)^{1/3} (n_g^2 - s^2)^{1/2} h_1(q_o) \quad (10)$$

$$q_z = \left(\frac{2}{ak}\right)^{-2/3} \left(1 + \frac{2}{a} z - s\right)^2 \quad (11)$$

$$H_j(q) = h_j'(q) + \frac{1}{2} \left(\frac{2}{ak}\right)^{2/3} h_j(q) ; j = 1, 2 \quad (12)$$

$$n_z^2 = 1 + \frac{2}{a} z \quad (13)$$

$$n_g^2 = \frac{\epsilon}{\epsilon_o} - i \frac{\sigma}{\epsilon_o} \quad (14)$$

$$D_{11} = \{F_1 h_1(q_d) + F_2 h_2(q_d)\}^2 \quad (15)$$

$$D_{12} = \{F_1 h_1(q_d) + F_2 h_2(q_d)\} \{F_3 h_1(q_d) + F_4 h_2(q_d)\} \quad (16)$$

$$D_{22} = \{F_3 h_1(q_d) + F_4 h_2(q_d)\}^2 \quad (17)$$

where ϵ/ϵ_o = dielectric constant of the ground and σ = the ground conductivity.

The subscripts on q and n represent the value of z at which these quantities are evaluated. The functions h_1 and h_2 are modified Hankel functions of order $1/3$ as defined in reference 8. The primes on these quantities denote derivatives with respect to the argument.

The modal excitation factor and height gain functions are needed in computing electric field strengths. The excitation factors of table 1 must be supplemented with the height gain functions which are given in reference 1 as:

$$f_1(z) = \exp\left(\frac{z}{a}\right) \{F_1 h_1(q) + F_2 h_2(q)\} \quad (18)$$

$$f_2(z) = \{F_3 h_1(q) + F_4 h_2(q)\} / \{F_3 h_1(q_o) + F_4 h_2(q_o)\} \quad (19)$$

$$f_3(z) = \frac{1}{ik} \frac{df_1}{dz} \quad (20)$$

where f_1 is the height gain for the vertical electric field E_z , f_2 is the height gain for the horizontal electric field component E_y , and f_3 is the height gain for the horizontal electric field component E_x .

The basic mode sum equation is given by

$$E = \frac{\eta}{4\pi} \left(\frac{2\pi p}{10k} \right)^{1/2} \frac{k}{2} \frac{\sum E_m}{[a \sin(x/a)]^{1/2}} \quad (21)$$

where E = total electric field in volts/metre

E_m = complex amplitude of each mode

p = power radiated

η = free-space impedance

If the waveguide is homogeneous in the direction of propagation, then E_m is given by

$$E_m = A_m \exp \{-ik S_m x\} \quad (22)$$

where A_m is the complex amplitude of the m th mode to be described later. If the parameters A_m and S_m are slowly varying functions of distance, then the so-called WKB form of E_m is given by references 1 and 9 as

$$E_m = A_m(x) \exp \{-ik \int_0^x S_m(\rho) d\rho\} \quad (23)$$

where

$$\begin{aligned}\Lambda_m &= \{[\lambda_{zr}^m(0) \lambda_{zr}^m(x)]^{1/2} g_z(z_t) \cos\gamma \\ &+ [\lambda_{yr}^m(0) \lambda_{yr}^m(x)]^{1/2} g_y(z_t) \sin\gamma \sin\theta \\ &+ [\lambda_{xr}^m(0) \lambda_{xr}^m(x)]^{1/2} g_x(z_t) \sin\gamma \cos\theta\} g_r(z_r)\end{aligned}\quad (24)$$

and r denotes the orientation of the received electric field component. If equation 24 is used, then equation 26 reduces to

$$\begin{aligned}\Lambda_m &= \{\lambda_{zr}^m g_z(z_t) \cos\gamma \\ &+ \lambda_{yr}^m g_y(z_t) \sin\gamma \sin\theta \\ &+ \lambda_{xr}^m g_x(z_t) \sin\gamma \cos\theta\} g_r(z_r)\end{aligned}\quad (25)$$

WKB IMPLEMENTATION

The procedure implemented in the WKBFLDS computer program is to segment the earth-ionosphere waveguide into M cascaded uniform waveguides as shown in figure 2. These segments (or slabs) are numbered from left to right. Slab 1 contains the transmitter. The distance from the transmitter to the beginning of each slab is denoted by ρ_k . The waveguide parameters associated with each slab are determined by the user based on consideration of the variations of the path conditions (geomagnetic field, ground conductivity, and the ionospheric profiles of electron density, ion density, and collision frequency).

The mode generating programs (ref 6 or 7) are run to obtain as many modes as desired in each slab. The WKB model requires an equal number of modes in each slab and the modes must be traced from one slab to the next in order to preserve mode numbers. At each slab boundary energy is transferred from a given mode into the corresponding mode in the next slab. The values of Λ_m and S_m at the beginning of each segment are defined to be those obtained from the full-wave programs. The values of each quantity within each segment are obtained by linear interpolation between the values at the segment bound-

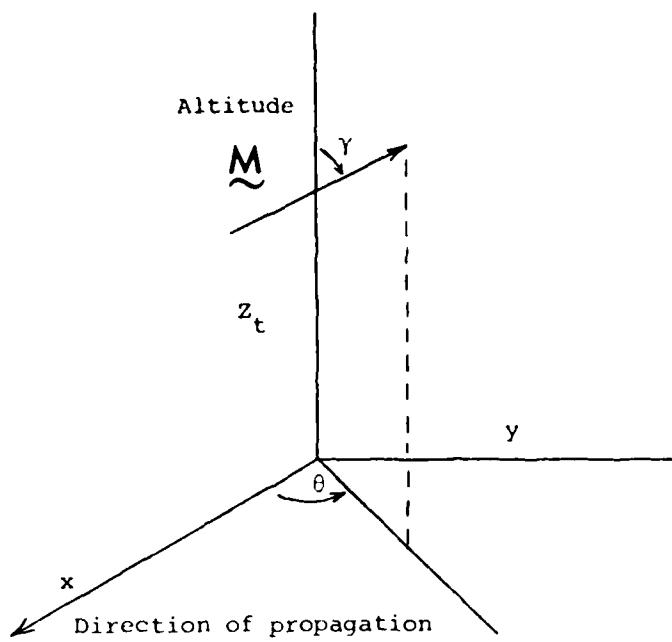


Figure 1. Dipole orientation within the waveguide

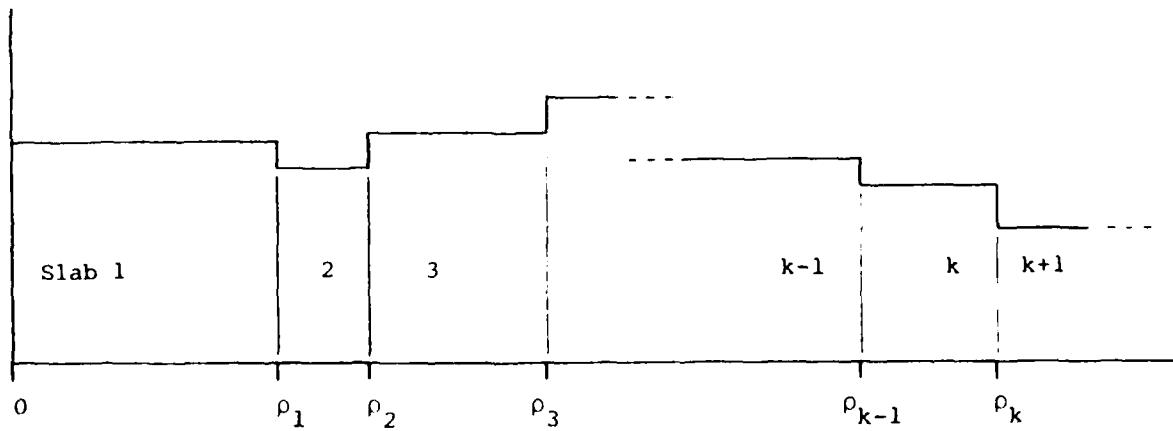


Figure 2. Diagram illustrating propagation path segmentation

aries. Care is taken to insure continuity of the phase of A_m and S_m from the transmitter to the receiver.

PROGRAM EXECUTION

OPTIONS

The program has three output options. For compatibility with other programs these options are numbered 1, 2, and 4. Option 1 produces fields as functions of distance parametric in transmitter altitude and orientation for a fixed receiver altitude and orientation. The program generates 501 points between the transmitter (distance = 0) and the end of the path (distance = DMAX, described below). The calculated fields and appropriate constants may be written to logical file 2 for processing by other programs. The calculated amplitude and relative phase may be printed and/or plotted. The vertical and horizontal (distance) dimensions and scales of the plots may be arbitrarily specified. Each set of distance calculations can be made for up to 20 transmitter orientations.

Option 2 produces fields as functions of a transmitter's position in an orbit for a fixed transmitter altitude and antenna inclination and for a fixed receiver altitude and orientation. The program generates 73 points between $\theta = 0^\circ$ and $\theta = 360^\circ$. Up to three different orbit configurations may be obtained: a dipole rotating in a counterclockwise direction, and clockwise and counterclockwise orbiting at a specified radius. Clockwise is determined by looking down the z-axis towards the x-y plane. Each set of orbit calculations is made at as many as 20 different distances from the transmitter. The calculated amplitude and relative phase may be printed. The results are always plotted using a fixed vertical size and scale and a user specified horizontal size.

Option 4 produces fields as functions of distance for fixed values of the transmitter and receiver altitudes and orientations. The data sets are varied so as to produce comparison plots. The printed and plotted outputs are all specified as for option 1. The procedure for storing the calculated fields on an external device is also provided as for option 1.

CONTROL CARDS

The flow of program execution is controlled by a set of cards which define the type of data being input and allow standard defaults to apply. All 80 columns of these control cards are read and printed. However, only the first four columns are examined by the program. Thus the input card and the printout can contain additional comments. For example, "NAMELIST DATA FOR AN ELEVATED TRANSMITTER" can be used in place of the minimum requirement of "NAME". The control cards are described below and a sample set is shown in figure 3.

<u>NAME</u>	Signals that NAMELIST data follow. The NAMELIST name is DATUM. The NAMELIST variables are described below.
IOPT	Option number - DEFAULT = 1
ICOMP	Index of received electric field component = 1 gives the vertical field (z) - DEFAULT = 2 gives the horizontal transverse field (y) = 3 gives the horizontal longitudinal field (x)
TALT	Transmitter altitude in km (ie, z_t) - DEFAULT = 0.0
RALT	Receiver altitude in km (ie, z_r) - DEFAULT = 0.0
INCL	Transmitting antenna inclination in degrees (ie, γ). This is an array of 20 elements - DEFAULT = 0.0
THETA	Transmitting antenna azimuth in degrees (ie, θ). This is an array of 20 elements - DEFAULT = 0.0
NRA	Number of pairs of INCL and THETA to be used. This applies only to option 1 - DEFAULT = 1
DIST	Distance between an orbiting transmitter and a receiver in Mm. This is an array of 20 elements - DEFAULT = 1.0
NRD	Number of values of DIST to be used. This applies only to option 2 - DEFAULT = 1
NRDATA	Number of input data sets to process for option 4 - DEFAULT = 1
RADIUS	Radius of the orbit in Mm used in option 2 - DEFAULT = 0.0
POWER	Total radiated power in kW - DEFAULT = 1.0

NPRINT Printout control flag
 = 0 generates a minimum of print
 = 1 generates full print (described in example data section) -
 DEFAULT
NAPLOT Amplitude plot flag
 = 0 deletes plot
 = 1 generates plot - DEFAULT
 = 0 deletes plot - DEFAULT
 = 1 generates plot
NPDIFF Phase difference plot flag
 = 0 deletes plot - DEFAULT
 = 1 generates plot
NRCURV Number of curves to be plotted per graph for option 1 and 4 -
 DEFAULT = 4
SIZEX Length of the horizontal plot axis for current option in inches
 (for all options) - DEFAULT = 10.0
SIZEY Length of the vertical axis for current option in inches (for
 options 1 and 4 only) - DEFAULT = 9.0
SIZEX1 Length of axis for option 1 and 4 only - DEFAULT = 10.0, 8.0
SIZEY1
SIZEX2 Lengths of axes for option 2 only - DEFAULT = 1.0, 4.0 (note
 that SIZEY2 is included for completeness only, the value cannot
 be changed)
AMPMAX Maximum value of amplitude to be plotted in dB above 1 μ V/m for
 options 1 and 4 - DEFAULT = 70.0
AMPMIN Minimum value of amplitude to be plotted - DEFAULT = -10.0
AMPINC Tic mark intervals for amplitude axis in dB - DEFAULT = 10.0
PHSMAX Maximum positive phase excursion to be plotted in degrees for
 options 1 and 4 - DEFAULT = 360.0
PHSMIN Maximum negative phase excursion to be plotted - DEFAULT =
 -360.0
PHSINC Tic mark intervals for phase axis in degrees - DEFAULT = 90.0
DMAX Maximum distance of plot axis in Mm for options 1 and 4 -
 DEFAULT = 10.0
DMIN Minimum distance in Mm - DEFAULT = 0.0
XINC Tic mark intervals for distance axis in Mm - DEFAULT = 1.0

TOTAPE Integer flag for writing calculated fields to logical unit 2
 = 0 deletes output - DEFAULT
 = 1 generates output
 TLONG Transmitter longitude (written to logical unit 2 when TOTAPE = 1) - DEFAULT = 0.0
 TLAT Transmitter latitude (written to logical unit 2 when TOTAPE = 1) - DEFAULT = 0.0
 RBEAR Geographic bearing from transmitter to receiver (written to unit 2 when TOTAPE = 1) - DEFAULT = 0.0

After reading the NAMELIST the program reads the next control card.

DATA Signals that the propagation path data follow. The format of these data is that which is produced by reference 7. The first card contains the data set identification. This card is used to supply a literal path description such as "HAWAII TO WAKE". This is followed by sets of mode constants, one for each path segment. The first card for each segment contains the starting distance (ρ), frequency (f), magnetic azimuth, codip and intensity, ground conductivity (σ), dielectric constant (ϵ/ϵ_0), and the nominal height of the free-space portion of the waveguide (h). Of these parameters, ρ , f , σ , and ϵ/ϵ_0 must appear. The magnetic parameters and h are included for reference. This card is followed by the mode constants, one pair for each mode, containing the following information:

1 θ T_1 T_2
 2 θ T_3 T_4

where 1 and 2 are sequencing indices, θ is the complex eigen-angle at the ground, and T_s are complex constants described below.

$$T_1 = \frac{s^{1/2} (1 + \frac{-R}{\|R\|})^2 (1 - \frac{R_1}{\|R\|} \frac{\bar{R}_1}{\|R\|})}{F'(0_j) \frac{-R}{\|R\|} D_{\|}} \quad (26)$$

$$T_2 = \frac{s^{1/2} (1 + \frac{\bar{R}_1}{\|R\|})^2 (1 - \frac{R_1}{\|R\|} \frac{\bar{R}_1}{\|R\|})}{F'(\theta_j) \frac{\bar{R}_1}{\|R\|} D_{22}} \quad (27)$$

$$T_3 = \frac{s^{1/2} (1 + \frac{\bar{R}_1}{\|R\|}) (1 + \frac{\bar{R}_1}{\|R\|}) \frac{R_1}{\|R\|}}{F'(\theta_j) D_{12}} \quad (28)$$

$$T_4 = \frac{\frac{1}{\|R\|}}{\frac{1}{\|R\|}} \quad (29)$$

In terms of the Ts the elements of table 1 are given as:

$$(\lambda_{ij}) = \begin{pmatrix} T_1 S^2 & -T_3 S & T_1 S \\ -T_3 T_4 S & T_2 & -T_3 T_4 \\ -T_1 S & T_3 & -T_1 \end{pmatrix} \quad (30)$$

The list of modes for each segment is terminated by a blank card. A maximum of 30 modes will be used although there is no maximum number which the data deck may contain. The list of segments is terminated by a card with $\rho = 40$. Parameters for each segment are stored sequentially on logical file 3. The number of path segments is limited by the space allocated to this file. Each segment requires 1445 words of storage. After reading these data the program returns for another control card if the option is 1 or 2. If the option is 4, then the program generates the required calculations. Upon completion of these calculations, the program returns to read the next data set starting with the data set identification card. This cycle continues until NRDATA sets have been processed.

START Signals that all input is complete and initiates execution for options 1 and 2.

A sample of how the control cards may be used is shown in figure 3.

SPECIAL CONSIDERATIONS

The maximum value of NRCURV is 4 and the maximum number of modes is 30. If either of these values is exceeded, a message is printed and execution continues using the maximum value.

Option 1: Calculations all begin at the transmitter and end at DMAX. DMAX, DMIN, and XINC are used for the horizontal axis scaling.

Option 2: Scaling for amplitude and phase is done automatically. The range on the horizontal axis is 0° to 360° in orbit angle. If RADIUS = 0.0, only the rotating dipole calculations are made for counterclockwise rotation.

Option 4: NAMELIST input (specifying option 4 and NRDATA) must precede the DATA card. Each set of mode constants must be preceded by an identification card and not by a DATA card. Calculations all begin at transmitter and end at DMAX using the first value of INCL and THETA in each list.

TOTAPE = 1: Unit 2 receives the 500 values of the mode sum as single precision complex values, freq, TLONG, TLAT, RBEAR, POWER, INCL, THETA, TALT, RALT, DMIN, and DMAX (in that order). The output is written in unformatted form.

The procedure for using homogeneous sections along a path is to include a single card in the form 'R XX.XXX' after the appropriate segment data. This indicates that the previous set of mode constants are to be used at the distance given by XX.XXX on the card. As a special case, when running the program for the case of a horizontally homogeneous waveguide, mode constant data are input at 'R 0.0'. This is followed by a single card in the format 'R XX.XXX' where XX.XXX is the value of DMAX. Furthermore, the program allows for an instantaneous change in path mode constants. This is accomplished by using the same value of ρ for two consecutive sets of mode constants. This is used for minimizing the discrepancies generated by the program when the WKB assumption is violated, such as for large changes in ground conductivity. An example of the horizontally homogeneous sections is shown in the sample data set of figure 3.

```

1  NAME
2  &DATUM
3  IOPT=1,
4  INCL=0.,90., THETA=0.,90., NRA=2,
5  SIZEX=5., SIZEY=4.,
6  &END
7  DATA
8  TEST DATA
9  R 0.0  F 10.0  A 0.0  C 0.0  M 0.0  S 10.0  E 0.0
10 1 90.0  0.0  1 0.0  -4.70745100-002 0.0  -4.70745100-002
11 2 90.0  0.0  1 0.0  -2.35372600-002 1.0  0.0
12 1 81.93069 0.0  1 1.38439500-002-1.90354300-002 1.38439500-002-1.90354300-002
13 2 81.93069 0.0  1 6.92197500-003-9.51771500-003 1.0  0.0
14
15  R 5.0
16  R 5.0  F 10.0  A 0.0  C 0.0  M 0.0  S 10.0  E 0.0
17 1 90.0  0.0  1 0.0  -4.70745100-003 0.0  -4.70745100-003
18 2 90.0  0.0  1 0.0  -2.35372600-003 1.0  0.0
19 1 81.93069 0.0  1 1.38439500-003-1.90354300-003 1.38439500-003-1.90354300-003
20 2 81.93069 0.0  1 6.92197500-004-9.51771500-004 1.0  0.0
21
22  R 10.0
23  R 40.
24  START
25  NAME
26  &DATUM
27  ICOMP=2,
28  NPPLOT=1,
29  INCL=0.,90.,90.,THETA=0.,0.,90.,NRA=3,NRCURV=3,
30  &END
31  START
32  NAME
33  &DATUM
34  ICOMP=1,
35  IOPT=2,
36  INCL=45.,
37  DIST=4.9,5.1, NRD=2,
38  &END
39  START
40  NAME
41  &DATUM IOPT=4,NRDATA=2,NPPLOT=0,&END
42  DATA
43  TEST DATA
44  R 0.0  F 10.0  A 0.0  C 0.0  M 0.0  S 10.0  E 0.0
45 1 90.0  0.0  1 0.0  -4.70745100-002 0.0  -4.70745100-002
46 2 90.0  0.0  1 0.0  -2.35372600-002 1.0  0.0
47 1 81.93069 0.0  1 1.38439500-002-1.90354300-002 1.38439500-002-1.90354300-002
48 2 81.93069 0.0  1 6.92197500-003-9.51771500-003 1.0  0.0
49
50  R 5.0
51  R 5.0  F 10.0  A 0.0  C 0.0  M 0.0  S 10.0  E 0.0
52 1 90.0  0.0  1 0.0  -4.70745100-003 0.0  -4.70745100-003
53 2 90.0  0.0  1 0.0  -2.35372600-003 1.0  0.0
54 1 81.93069 0.0  1 1.38439500-003-1.90354300-003 1.38439500-003-1.90354300-003
55 2 81.93069 0.0  1 6.92197500-004-9.51771500-004 1.0  0.0
56
57  R 10.0
58  R 40.
59  TEST DATA WITH ALL AMPLITUDES REDUCED BY FACTOR OF 10
60  R 0.0  F 10.0  A 0.0  C 0.0  M 0.0  S 10.0  E 0.0
61 1 90.0  0.0  1 0.0  -4.70745100-003 0.0  -4.70745100-003
62 2 90.0  0.0  1 0.0  -2.35372600-003 1.0  0.0
63 1 81.93069 0.0  1 1.38439500-003-1.90354300-003 1.38439500-003-1.90354300-003
64 2 81.93069 0.0  1 6.92197500-004-9.51771500-004 1.0  0.0
65
66  R 5.0
67  R 5.0  F 10.0  A 0.0  C 0.0  M 0.0  S 10.0  E 0.0
68 1 90.0  0.0  1 0.0  -4.70745100-004 0.0  -4.70745100-004
69 2 90.0  0.0  1 0.0  -2.35372600-004 1.0  0.0
70 1 81.93069 0.0  1 1.38439500-004-1.90354300-004 1.38439500-004-1.90354300-004
71 2 81.93069 0.0  1 6.92197500-005-9.51771500-005 1.0  0.0
72
73  R 10.0
74  R 40.

```

Card column 1

Figure 3. Sample data deck

In order to facilitate mode matching across segment boundaries, a missing mode can be indicated by a pair of filler cards inserted in the deck where the mode would have appeared. This pair of cards must contain a non-zero eigen-angle value. Typically the eigenangle is the value from some previous segment which had the mode. The rest of each of the cards is blank.

EXAMPLE DATA

The data listed in figure 3 exercise the program in most of its options. The test data are fictitious. There are only two modes; their attenuation rate, phase velocity relative to the speed of light, and complex excitation factor Λ_{zz} are given in table 2.

Mode	Attenuation Rate dB/Mm	Phase velocity/c	$ \Lambda_{zz} $ dB	ϕ_{zz} in degrees
1	0	1.00	0	0
2	0	1.01	-6	36

Table 2. Test data mode parameters

These modes produce interference minima at 3 Mm intervals. The values of the Λ s of equations 28-31 are defined such that $\Lambda_{zz} = \Lambda_{yy} = \Lambda_{xx} = \Lambda_{xz} = \Lambda_{zx}$ and $\Lambda_{yz} = \Lambda_{zy} = \Lambda_{xy} = \Lambda_{yx} = 1/2 \Lambda_{zz}$ for each mode. Thus, a horizontal broadside antenna produces fields which are the same amplitude as produced by a vertical antenna. In figure 3, lines 1-6 are the NAMELIST input data specifying two transmitting antenna orientations: vertical and horizontal broadside. Lines 7-23 are the propagation path constants. Lines 15 and 22 illustrate the use of horizontally homogeneous segments. The first two pages of output for the calculations specified in lines 1-24 are shown in figures 4 and 5. In figure 4 we see the list of segment parameter cards after the control card DATA. After the control card START we see a listing of the mode parameters for each

R 5.000 F .0000 A .000 C .000 M .000 S .000 E .0
 USING DATA FROM PREVIOUS RHO
 R 5.000 F 10.000 A .000 C .000 M .000 S 1.000+001 E .0 MODES 2
 R 10.000 F .0000 A .000 C .000 M .000 S .000 E .0

LITERATURE REVIEW

2. CONVENTION 8012N 1

RHO	0.000	MODE	ATTEN	V/C	VERTICAL	BROADSIDE	END FIRE	V	B	E
1	.000	1.000000	-2.691	.000	-8.712	3.142	-75.238 -2.356	-2.69	-8.71	-75.24
	.000	1.010000	-8.885	.629	-14.819	-2.513	-81.345 -1.727	-8.88	-14.82	-81.35
2	.000	1.000000	-2.691	.000	-8.712	3.142	-75.238 -2.356	-2.69	-8.71	-75.24
	.000	1.010000	-8.885	.629	-14.819	-2.513	-81.345 -1.727	-8.88	-14.82	-81.35
5.000	.000	MODE	ATTEN	V/C	VERTICAL	BROADSIDE	END FIRE	V	B	E
	.000	1.000000	-2.691	.000	-8.712	3.142	-75.238 -2.356	-2.69	-8.71	-75.24
1	.000	1.000000	-2.691	.000	-8.712	3.142	-75.238 -2.356	-2.69	-8.71	-75.24
	.000	1.010000	-8.885	.629	-14.819	-2.513	-81.345 -1.727	-8.88	-14.82	-81.35
5.000	.000	MODE	ATTEN	V/C	VERTICAL	BROADSIDE	END FIRE	V	B	E
	.000	1.000000	-22.691	.000	-28.712	3.142	-95.238 -2.356	-12.69	-18.71	-85.24
1	.000	1.000000	-22.691	.000	-28.712	3.142	-95.238 -2.356	-12.69	-18.71	-85.24
	.000	1.010000	-28.885	.629	-34.819	-2.513	-101.345 -1.727	-18.88	-24.82	-91.35
10.000	.000	MODE	ATTEN	V/C	VERTICAL	BROADSIDE	END FIRE	V	B	E
	.000	1.000000	-22.691	.000	-28.712	3.142	-95.238 -2.356	-12.69	-18.71	-85.24
2	.000	1.000000	-22.691	.000	-28.712	3.142	-95.238 -2.356	-12.69	-18.71	-85.24
	.000	1.010000	-28.885	.629	-34.819	-2.513	-101.345 -1.727	-18.88	-24.82	-91.35

Figure 4. First page of output produced by lines 1-24 of sample deck

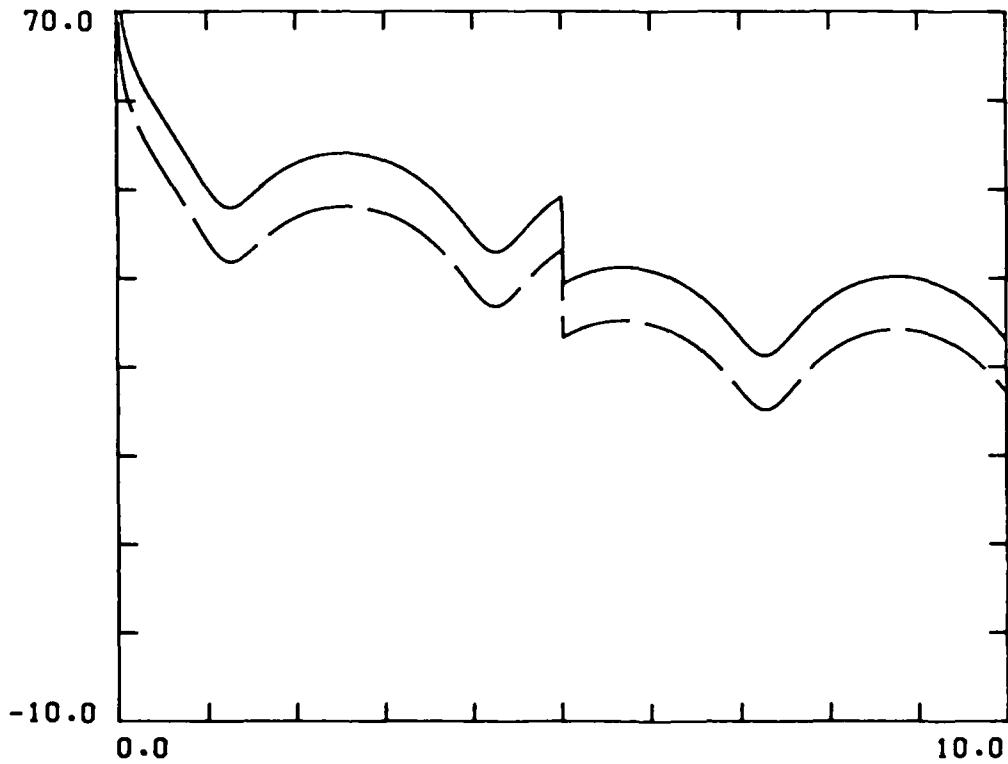
Figure 5. Second page of output produced by lines 1-24 of sample deck

segment. The headings "VERTICAL", "BROADSIDE", and "END FIRE" are for the magnitude in dB and phase in radians of the components of the excitation factors. The headings "V", "B", and "E" are for the relative magnitude of these components at the beginning of each slab. This list appears only when ICOMP, TALT, RALT, or the mode parameters are changed. In figure 5 we see the list of computed amplitude in dB above 1 μ V/m and phase relative to the speed of light in degrees printed as functions of distance in Mm. This list is preceded by a line of print indicating the received field component, the transmitting antenna orientation, and the altitudes of the transmitter and receiver. The plots for these calculations are shown in figure 6.

Lines 25-31 of figure 3 call for the E_y fields and phase plots. Three transmitting antenna orientations are specified. The resulting plots of the amplitude and relative phase are shown in figures 7a and 7b, respectively. There are apparently only two curves in figure 7a because the amplitude of E_y from a vertical source is the same as that from a horizontal end-fire source.

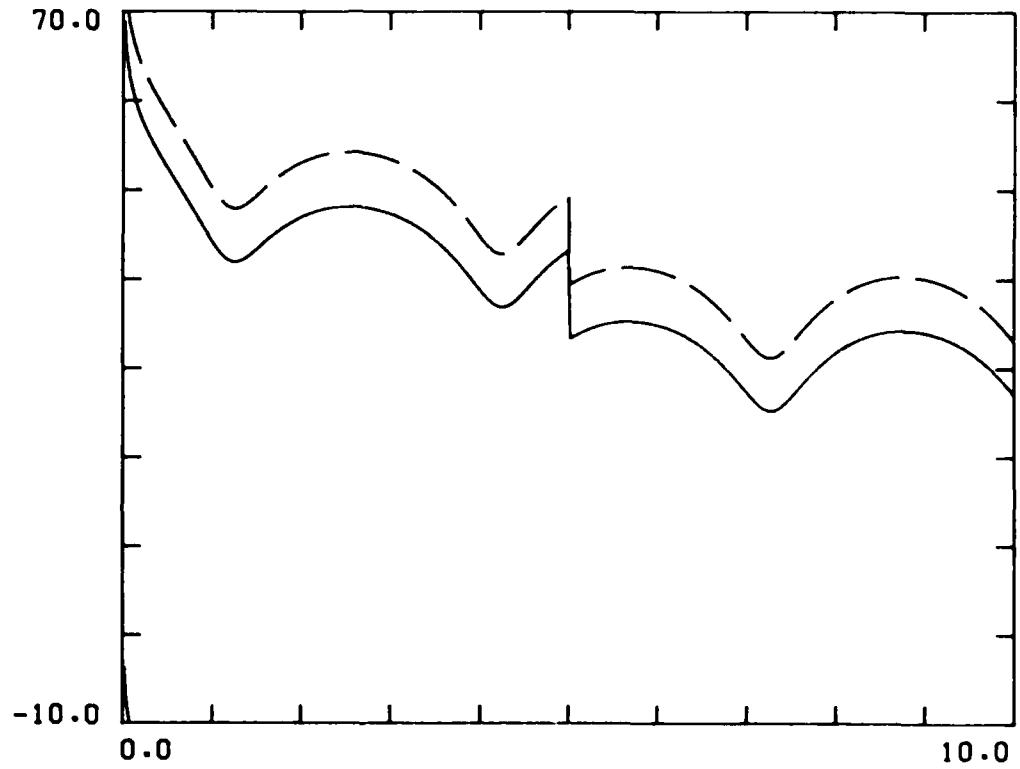
Lines 32-39 of figure 3 call for a rotating transmitter antenna inclined at 45°. The calculations are to be made for two distances. The first page of printout generated by these lines is shown in figure 8. The mean signal and the standard deviation of the signal for the rotation are printed at each distance. The table of amplitude and relative phase as a function of rotation angle, R, appears as a result of NPRINT = 1. The plots resulting from the calculations are shown in figure 9.

Lines 40-74 of figure 3 illustrate the IOPT = 4 option. The plots resulting from these calculations are shown in figure 10.



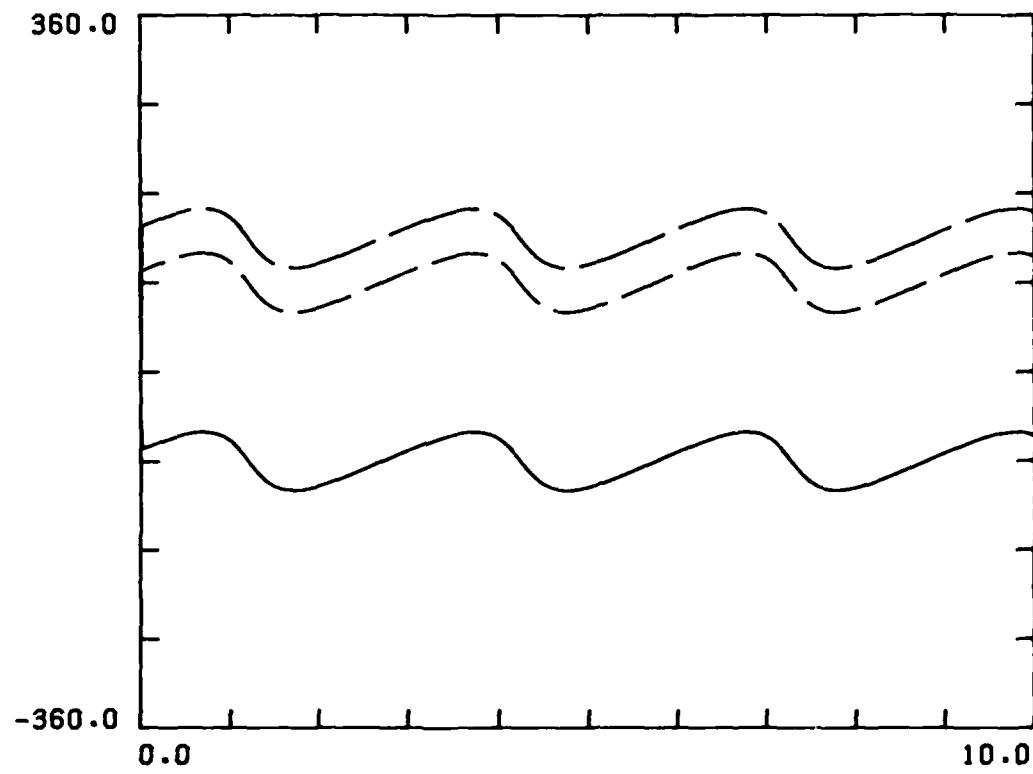
0.0 10.0
FLD4 1 050481 100348
AMPLITUDE
Z COMPONENT FREQ = 10.000 POWER = 1.0
TALT = 0.0 RALT = 0.0
TEST DATA
INCL = 0.000 THETA = 0.000
INCL = 90.000 THETA = 90.000

Figure 6. Plotted output generated by lines 1-24 of the sample deck



FLD4 2 050481 100348
AMPLITUDE
Y COMPONENT FREQ = 10.000 POWER = 1.0
TALT = 0.0 RALT = 0.0
TEST DATA
===== INCL = 0.000 THETA = 0.000
===== INCL = 90.000 THETA = 0.000
===== INCL = 90.000 THETA = 90.000

Figure 7a. Plotted amplitude output generated by lines 25-31 of the sample dec:



FL04 3 050481 100348
 RELATIVE PHASE
 Y COMPONENT FREQ = 10.000 POWER = 1.0
 TALT = 0.0 RALT = 0.0
 TEST DATA
 INCL = 0.000 THETA = 0.000
 INCL = 90.000 THETA = 0.000
 INCL = 90.000 THETA = 90.000

Figure 7b. Plotted relative phase output generated by lines 25-31 of the sample deck

```

NAME
$DATUM
1OPT = 2,1COMP = 1,TALT = .00000000 'RALT = .00000000
TLONG = .00000000 'RLAT = .00000000 'RBAR = .00000000
SIZE1 = .40000000+001,SIZEY1 = .40000000+001,SIZEY = .10000000+001,TOTAPE =
SIZE2 = .10000000+001,SIZE2 = .40000000+002,AMPPMAX = .10000000+002,AMPPMIN =
AMPINC = .10000000+002,PHSMAX = .36000000+003,PHSMIN = .36000000+003,PHSINC =
DMIN = .00000000 'XINC = .90000000+001,NRCURV =
NPDIFF = .00000000 'RADIUS = .00000000
DIST = .49000000+001,51000000+001,00000000 '00000000 00000000 00000000
.00000000 '00000000 '00000000 '00000000 '00000000 '00000000
.00000000 '00000000 '00000000 '00000000 '00000000 '00000000
INCL = .45000000+002,90000000+002,90000000+002,NRD =
.00000000 '00000000 '00000000 '00000000 '00000000 '00000000
.00000000 '00000000 '00000000 '00000000 '00000000 '00000000
.00000000 '00000000 '00000000 '00000000 '00000000 '00000000
.00000000 '00000000 '00000000 '00000000 '00000000 '00000000
.00000000 '00000000 '00000000 '00000000 '00000000 '00000000
.00000000 '00000000 '00000000 '00000000 '00000000 '00000000
THETA = .00000000 '00000000 '00000000 '00000000 '00000000 '00000000
.00000000 '00000000 '00000000 '00000000 '00000000 '00000000
.00000000 '00000000 '00000000 '00000000 '00000000 '00000000
SEND

```

START

2 COMPONENT OPTION 2

```

2 COMP DIST = 4.900 INCL = 45.000
THETA AMPLITUDE PHASE
45.4393 61.9779 95.000 39.4417 62.2505
5.000 45.0517 61.9895 100.000 39.5402 62.2462
10.000 44.6492 62.0022 105.000 39.7009 62.2382
15.000 44.2337 62.0160 110.000 39.9193 62.2269
20.000 43.8077 62.0309 115.000 40.1894 62.2130
25.000 43.3741 62.0470 120.000 40.5045 62.1969
30.000 42.9364 62.0642 125.000 40.8573 62.1793
35.000 42.4987 62.0823 130.000 41.2404 62.1608
40.000 42.0659 62.1013 135.000 41.6466 62.1418
45.000 41.6434 62.1210 140.000 42.0692 62.1228
50.000 41.2373 62.1409 145.000 42.5021 62.1042
55.000 40.8544 62.1608 150.000 42.9398 62.0861
60.000 40.5019 62.1801 155.000 43.3774 62.0689
65.000 40.1872 62.1983 160.000 43.8110 62.0525
70.000 39.9174 62.2147 165.000 44.2369 62.0371
75.000 39.6995 62.2287 170.000 44.6523 62.0227
80.000 39.5392 62.2397 175.000 45.0548 62.0093
85.000 39.4412 62.2472 180.000 45.4423 61.9970
90.000 39.4084 62.2508 185.000 45.8132 61.9855
DIST MEAN A STD 3.328
4.900 44.845

```

2 COMP DIST = 5.100 INCL = 45.000
THETA AMPLITUDE PHASE
36.7202 66.5690 95.000 30.7138 66.7683
5.000 36.3322 66.5773 100.000 30.8125 66.7657
10.000 35.9293 66.5863 105.000 30.9736 66.7604
15.000 35.5133 66.5961 110.000 31.1924 66.7527
20.000 35.0868 66.6068 115.000 31.4630 66.7430

Figure 8. First page of printout generated by lines 32-39 of the sample deck

FLD4 4 050481 100348

TEST DATA

Z COMPONENT

FREQ = 10.000 POWER = 1.0

T ALT = 0.0 R ALT = 0.0

INCL = 45.000

RADIUS = 0.0000

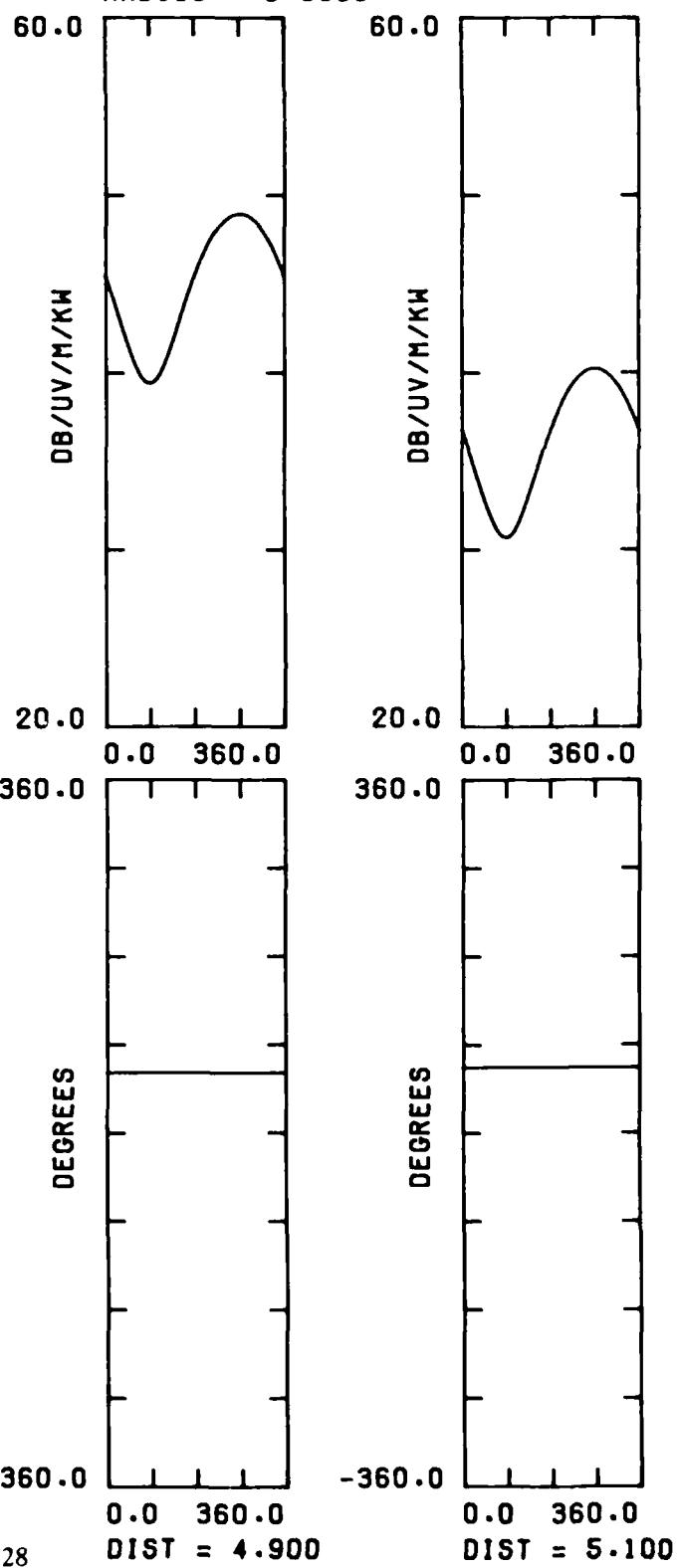
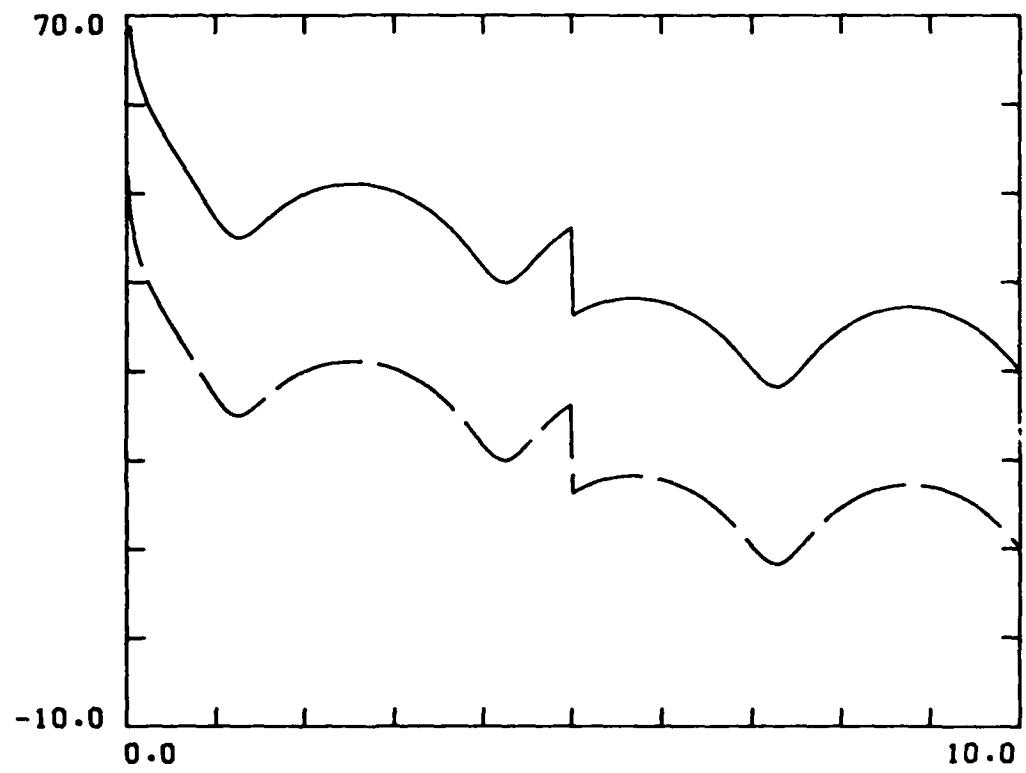


Figure 9. Plotted output generated by lines 32-39 of the sample deck



FLD4 5 050481 100348
AMPLITUDE
Z COMPONENT FREQ = 10.000 POWER = 1.0
TALT = 0.0 RALT = 0.0
INCL = 45.000 THETA = 0.000
TEST DATA
TEST DATA WITH ALL AMPLITUDES REDUCED BY FACTOR OF 10

Figure 10. Plotted output generated by lines 40-74 of the sample deck

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3. Wait, JR, Electromagnetic Waves in Stratified Media, Macmillan, New York, 1962
4. Galejs, J, Terrestrial Propagation of Long Electromagnetic Waves, Pergamon Press, Oxford, 1972
5. NELC Interim Report 683, A Fortran Program for Mode Constants in an Earth-Ionosphere Waveguide, by CH Shedd, RA Pappert, Y Gough, and WF Moler, 1968
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8. Wait, JR, Two-dimensional Treatment of Mode Theory of the Propagation of VLF Radio Waves, Radio Science Journal of Research, NBS/USNC-URSI Vol 68D, No 1, 1964
9. Computation Laboratory Staff at Cambridge, MA, Tables of the Modified Hankel Function of Order One-Third and of Their Derivatives, Harvard University Press, Cambridge, MA, 1945

APPENDIX: PROGRAM LISTING

```

1 2
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52 53
53 54
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55 56
56

C FLD4: WKB MODE SUM
C
$ COMMON/INPUT /STP(30),TP(30),AV(30),EX(3,3,30),EK,ALPHA,SIGMA,EPSR,
$ MODES, RHO
$ COMMON/DONE/RHOMAX,RHOD,NEWD,NEWHGT,NEWHGR,NEWP
$ COMMON/IDENT/ID(20),FREQ,TALI,RALT,ICOMP,ZYX,IOPT,THTA,INCANG,DST,
$ RADIUS, POWER
$ COMMON/DIMEN/XLNG,YLNG,AMPMAX,AMPMIN,AMPINC,PHSMAX,PHSMIN,
$ PHSINC,DMAX,DMIN,XINC,TMAX,TMIN,TINC,
$ NRCURV,NPLOT,NPDIFF,NPRINT
$ COMMON/OUTPUT/XY(501),AMP(501),PHS(501),NRPTS,NRCRVS,NRPLTS,
$ DATE, TIME
$ COMMON/NODEMODE(30)
C
C COMPLEX*16 TP,STP,AV,EX,MIK,RATIO,TMP1,TMP2,TMP3,TMP4
C COMPLEX*8 SUMOUT
C REAL*8 DTR/1.745329252D-2/,ALPHA/3.14D-4/,SIGMA,EPSR,
$ SC,SIN10,COS10,CC
$ REAL*4 INCL,INCANG,MAGFLD
$ INTEGER TOTAPE,0/
LOGICAL NOMODE
CHARACTER*8 DATE,TIME
CHARACTER*4 BCD,NAME,INPT,EXEC,ENDF
CHARACTER LABEL,ZYX
C
C DIMENSION BCD(20),LABEL(3),RATIO(4),SUMOUT(501)
$ DIST(20),INCL(20),THETA(20),SINT(73),SC(3,73)
C
C NAMELIST/DATUM/IOPT,ICOMP,TALT,POWER,TOTAPE,TLONG,TLAT,RBEAR,
$ SIZEX,SIZEY,
$ SIZEX1,SIZEX2,SIZEY1,SIZEY2,AMPMAX,AMPMIN,AMPINC,PHSMAX,
$ PHSINC,DMAX,DMIN,XINC,NRCURV,NPRINT,NPLOT,
$ NPLOT,NPDIFF,RADIUS,DIST,NRD,INCL,THETA,NRA,NRDATA
C...COMMON INITIALIZATION
C DATA AMPMAX/70./,AMPMIN/-10./,PHSMAX/360./,PHSMIN/-360./
C DATA DMAX/10./,DMIN/0./,TMAX/360./,TMIN/0./
C DATA TALT,RALT/0.,0./,ICOMP/1./,RADIUS/0./,POWER/1./
C DATA NRCURV/4./,NPLOT/1./,NPDIFF/0./
C DATA NPRINT/1./
C DATA AMPINC/10./,PHSINC/90./,XINC/1./
C DATA ICOMPS/0./,NRCRVS/0./,NRPLTS/0./,NEWD/-1/
C
C DATA INPT/4HDATA/,NAME/4HNAME/,EXEC/4HSTAR/,ENDF/4HENDF/
$ LABEL/'Z','Y','X',STALT,SRALT/2*-1./,IOPT/1/,NRDATA/1/,
$ SIZEX/-1./,SIZEY/-1./,
$ SIZEY1/10./,SIZEY2/8./,NRPTS1/501/,
$ SIZEX2/1./,SIZEY2/4./,NRPTS2/73/,
$ DIST,INCL,THETA/1.,59*0./,NRD,NRA/2*1./,TLONG,TLAT,RBEAR/3*0./
C
C CALL DATE(DATE,TIME)
C PRINT 999,DATE,TIME
C ..READ AND TEST CONTROL CARD
1G PRINT 1005

```

```

57 11 READ(5,1001,END=990) BCD
58   PRINT 1002,BCD
59   IF (BCD(1) .EQ. NAME) GO TO 15
60   IF (BCD(1) .EQ. EXEC) GO TO 30
61   IF (BCD(1) .EQ. INPT) GO TO 20
62   IF (BCD(1) .EQ. ENDF) GO TO 56
63   GO TO 910

64 C...READ AND PRINT NAMELIST DATA
65 READ(5,DATUM,END=989)
66   PRINT DATUM
67   IF (NRCURV .GT. 4) GO TO 908
68   IF (SIZEX .LT. 0) GO TO 160
69   GO TO (151,152,912,151),10PT
70   151 SIZEX1=SIZEX
71   GO TO 159
72   SIZEX2=SIZEX
73   SIZEX=-1.
74   159 SIZEX=1.
75   160 IF (SIZEY .LT. 0.) GO TO 170
76   GO TO (161,169,912,161),10PT
77   161 SIZEY1=SIZEY
78   169 SIZEY=-1.
79   170 IF (SIZEY1 .GT. 0.) GO TO 913
80   GO TO 11

81 C...READ PROPAGATION PATH PARAMETERS
82 C...SET COUNTER FOR 10PT=4
83 C...SET COUNTER FOR 10PT=4
84 C...SET COUNTER FOR 10PT=4
85 20  NDATA=0
86 200 READ(5,1001,END=989) 10
87   PRINT 1002,10
88   REWIND 3
89   MNMODE=31
90   NR=0
91   RHO=-1.

92 C...READ SEGMENT CONSTANTS
93 21  READ(5,1020,END=989) R,F,A,C,B,S,E
94   IF (R .EQ. 40.) GO TO 25
95   B=B*10000.
96   PRINT 1021,R,F,A,C,B,S,E
97   IF (NPRINT .LT. 2) GO TO 210
98   PRINT 1221
99   210 IF (NR .GT. 0) GO TO 22
100  FREQ=F
101  C   WN=2*PI*FREQ/C
102  103  WN=20.958445E0*FREQ
104  104  MIK=CMPLX(0.,-WN)
105  105  EK=682.2408*SQRT(FREQ)
106  22   NR=NR+1
107  107  IF (RHO .GT. 0) GO TO 911
108  108  RHO=R
109  109  RHOMX=R
110  110  C...CHECK IF THIS IS JUST A RHO CARD - FOR HOMOGENEOUS SEGMENT
111  111  IF (S .GT. 0.) GO TO 220
112  112  PRINT 1220
113  113  GO TO 241

```

```

114 220  SIGMA=S
115  EPSR=E
116  AZIM=A
117  CODIP=C
118  MAGFLD=B
119
C...READ MODE CONSTANTS
120
121  NM=0
122  READ(5,1023,END=989) INDX1,TR1,T11,TMP1,TMP2
123  IF (TR1 .EQ. 0.) GO TO 24
124  NM=1NM+1
125  READ(5,1023,END=989) INDX2,TR2,T12,TMP3,TMP4
126  IF (NPRINT .LT. 2) GO TO 223
127  PRINT 1025, NM,INDX1,TR1,T11,TMP1,TMP2,INDX2,TR2,T12,TMP3,TMP4
128  IF (TR1 .NE. TR2 .OR. T11 .NE. T12) GO TO 919
129  IF (INDX1 .EQ. INDX2) GO TO 919
130  IF (INDX1 .NE. 1 .AND. INDX1 .NE. 2) GO TO 919
131  IF (INDX2 .NE. 1 .AND. INDX2 .NE. 2) GO TO 919
132  C...TEST IF MAXIMUM NUMBER OF MODES EXCEEDED
133  IF (NM .GT. 30) GO TO 23
134  TP(NM)=IMPLX(TR1,T11)
135  STP(NM)=CDSIN(TP(NM)*DTR)
136  AV(NM)=NIK*(STP(NM)-1.0D0)
137  C...TEST FOR MISSING MODE
138  NCNODE(NM)= FALSE.
139  IF (CDANS(TMP1) .NE. 0.0D0) GO TO 230
140  NODQUE(NM)= .TRUE.
141  TMP1=1.D-20
142  TMP2=1.D-20
143  TMP3=1.D-20
144  TMP4=1.D0
145  230  RATIO(2*INDX1-1)=TMP1
146  RATIO(2*INDX1 )=TMP2
147  RATIO(2*INDX2-1)=TMP3
148  RATIO(2*INDX2 )=TMP4
149  C...DEFINE EXCITATION FACTOR MATRIX
150  EX(1,1,NM)= RATIO(1*STP(NM)**2)
151  EX(2,1,NM)= -RATIO(3*RATIO(4)*STP(NM))
152  EX(3,1,NM)= -RATIO(1*STP(NM))
153  EX(1,2,NM)= -RATIO(3*STP(NM))
154  EX(2,2,NM)= RATIO(2)
155  EX(3,2,NM)= RATIO(3)
156  EX(1,3,NM)= RATIO(1*STP(NM))
157  EX(2,3,NM)= -RATIO(3*RATIO(4)
158  EX(3,3,NM)= -RATIO(1)
159  GO TO 23
160  24  IF (NM .EQ. 0) GO TO 909
161  IF (NPRINT .NE. 2) PRINT 1026,NM
162  IF (NM .GT. 30 .OR. NM .GT. MNMODE) PRINT 1014
163  MODES=MINO(30,NM)
164  MODES=MINO(MODES,MNNQUE)
165  C...SAVE SEGMENT DATA
166  WRITE(3) STP,TP,AV,EX,SIGMA,EPSR,RHO,MODES,NODE
167  MNMODE=MODES
168  GO TO 21
169  IF (NR .LE. 1) GO TO 915
170

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```

171      NEWD=1
172      NDATA=NDATA+1
173      IF (IOPT .EQ. 4) GO TO 30
174      GO TO 11
175
176      IF (NEWD .EQ. -1) GO TO 916
177      ZYXZLABEL (ICOMP)
178      PRINT 1004,ZYX,IOPT
179
C...CHECK IF NEW HEIGHT GAIN CALCULATIONS ARE NEEDED
180      NEWP=0
181      NEWHGT=0
182      IF (ICOMP .EQ. ICOMP .AND. NEWD .EQ. 0) GO TO 36
183      NEWP=1
184      ICOMP='COMP
185      IF (TLAT .EQ. STALT .AND. NEWD .EQ. 0) GO TO 40
186      NEWP=1
187      NEWHGT=1
188      STALT=TLAT
189      IF (TLAT .EQ. STALT .AND. NEWD .EQ. 0) GO TO 41
190      NEWP=1
191      NEWHGR=1
192      SRALT=TLAT
193
C...BRANCH TO OPTION
194      41      GO TO (50,60,912,90),IOPT
195
C...FIELDS VS DISTANCE PARAMETRIC IN INCL AND THETA
196
197      50      NRPTS=NRPTS1
198      NRPTS=NRPTS1
199      XLNG=SIZEY1
200      YLNG=SIZEY1
201      XYMAX=AMIN (DMAX,RHOMAX)
202      DINC=(XYMAX-DMIN)/(NRPTS-1)
203      XY(1)=DMIN
204      DU 52  J=2,NRPTS
205      XY (J)=XY (J-1)+DINC
206      C...LOOP OVER ANTENNA ORIENTATIONS
207      DO 55  I=1,NRA
208      INCANG=INCL(I)
209      THTA=THETA(I)
210      SC (1,1)=DCOS (INCANG*DTR)
211      SIN0=DSIN (INCANG*DTR)
212      SC (2,1)=SIN0*DSIN (THTA*DTR)
213      SC (3,1)=SIN0*DCOS (THTA*DTR)
214      RHOD=0.
215      C...LOOP OVER DISTANCE
216      DO 54  J=1,NRPTS
217      CALL SUMS (J,XY (J),AMP (J),PHS (J),SUMCUT (J),SC (1,1),0.)
218      54      CONTINUE
219      NEWP=0
220      NEWD=0
221      NEWHGT=0
222      NEWHGR=0
223      CALL RPUT1 (I,NRA)
224      IF (TOTAPE .EQ. 1) WRITE (2) SUMOUT,FREQ,TLONG,TLAT,RBEAR,POWER,
225      $ INCANG,THTA,TLAT,RALT,DMIN,XYMAX
226      IF (DMAX .LT. RHOMAX) NEWHGR=1
227      GO TO 10

```

```

226 50  IF(TOTAPE .EQ. 1) END FILE 2
229 51  GO TO 1;
230 52  C...FIELDS VS THETA PARAMETRIC IN DISTANCE
231 53  NRPTS=NRPTS2
232 54  XLNG=SIZEX2
233 55  YLNG=4.
234 56  IMAX=NRD-1
235 57  IF(NRD .EQ. 1) GO TO 420
236 58  C...MAKE SURE DISTANCES ARE IN ORDER OF INCREASING VALUE
237 59  IF(DIST(J) .GT. DIST(I)) GO TO 42
238 60  DO 42 I=1,IMAX
239 61  JMIN=I+1
240 62  DO 42 J=JMIN,NRD
241 63  IF(DIST(J) .LE. DIST(I)) GO TO 42
242 64  TEMP=DIST(J)
243 65  DIST(J)=DIST(I)
244 66  DIST(I)=TEMP
245 67  CONTINUE
246 68  C...MAKE SURE DISTANCES ARE NOT BEYOND END OF DATA
247 69  DO 43 J=1,NRD
248 70  IF(DIST(J) .LE. RHOMAX) GO TO 43
249 71  NRD2=J-1
250 72  IF(NRD2 .EQ. 0) GO TO 421
251 73  PRINT 1017,RHOMAX
252 74  GO TO 44
253 75  PRINT 1018
254 76  GO TO 10
255 77  43  CONTINUE
256 78  C...SET UP ANTENNA ORIENTATION PARAMETERS
257 79  NRD2=NRD
258 80  INCANG=INCL(1)
259 81  INCIO=DSIN(INCANG*DTR)
260 82  COSIO=DCOS(INCANG*DTR)
261 83  TINC=(MAX-TMIN)/(NRPTS-1)
262 84  XY(1)=0.
263 85  SIN(1)=0.
264 86  SC(1,1)=COSIO
265 87  SC(2,1)=0.D0
266 88  SC(3,1)=SINIO
267 89  DO 6; J=2,NRPTS
268 90  XY(J)=XY(J-1)+TINC
269 91  SIN(J)=DSIN(XY(J)*DTR)
270 92  SC(1,J)=COSIO
271 93  SC(2,J)=SINIO*DSIN(XY(J)*DTR)
272 94  SC(3,J)=SINIO*DCOS(XY(J)*DTR)
273 95
274 96  C...SET UP PLOT
275 97  CALL PLOT(1.5,.5,-3)
276 98  NEWP=0
277 99  RHOD=0
278 100  IF(NPRINT .LT. 1) PRINT 1030
279 101  C...LOOP OVER DISTANCES
280 102  DO 68 I=1,NRD2
281 103  DST=DIST(I)
282 104  IF(DST .EQ. 0.) GO TO 68
283 105  C...LOOP OVER ORBITS
284

```

```

R=0.
CC= 1. DO
  286  DD 66  JJ=1,3
  287  DO OVER ANTENNA AZIMUTHS
  288
  289  DO 62  J=1, NRPTS
  290  SC(2,J)=CC*SC(2,J)
  291  82  CALL SUMS(J,DST,AMP(J),PHS(J),SUMOUT(1),SC(1,J),R*SINT(J))
  292  NEND=0
  293  NEWHGT=0
  294  CALL POUT2(JJ,1)
  295  IF(JJ .GT. 1) GO TO 65
  296  SUM1=0.
  297  83  SUM1=SUM1+AMP(J)
  298  AM=SUM1/NRPTS$
  299  SUM1=0.
  300  64  J=1,NRPTS
  301  SUM1=SUM1+(AMP(J)-AM)**2
  302  64  AS=SQRT(SUM1/(NRPTS$-1))
  303  IF(NPRINT .GT. 0) PRINT 1030
  304  PRINT 1031,DST,AM,AS
  305  85  IF(RADIUS .EQ. 0.) GO TO 67
  306  R=RADIUS
  307  CC=-1. DO
  308  66  CONTINUE
  309  67  CALL PLOT(XLNG+1, 0., -3)
  310  67  CONTINUE
  311  68  CALL PLOT(0., 0., -4)
  312  68  IF(DST .GE. RHOMAX) NEWHGR=0
  313  68
  314  GO TO 10
  315  C...MULTIPLE DATA FOR SINGLE COMPONENT, TALT, RALT, INCL AND THETA
  316  90  IF(NDATA.GT. 1) GO TO 91
  317  NRPTS=NRPTS1
  318  XLNG=SIZEX1
  319  YLNG=SIZEY1
  320  INCANG=INCL(1)
  321  THTA=THETA(1)
  322  SC(1,1)=DCOS(INCANG*DTR)
  323  SIN10=DSIN(INCANG*DTR)
  324  SC(2,1)=SIN10*DSIN(THTA*DTR)
  325  SC(3,1)=SIN10*DCOS(THTA*DTR)
  326  RHOD=0.
  327  91  DINC=(AMIN1(DMAX,RHOMAX)-DMIN)/(NRPTS$-1)
  328  XY(1)=DMIN
  329  DD 92  J=2,NRPTS
  330  92  XY(J)=XY(J-1)+DINC
  331  DO 94  J=1,NRPTS
  332  CALL SUMS(J,XY(J),AMP(J),PHS(J),SUMOUT(J),SC(1,1),0.)
  333  94  CONTINUE
  334  94  IF(TOTAPE .EQ. 1) WRITE(2) SUMOUT(2),SUMOUT(1),FREQ,TLONG,TLAT,RBEAR,POWER,
  335  $ INCANG,THTA,TALT,RALT,DMIN,DMAX
  336  94  CALL POUT1(NDATA,NPDATA)
  337  IF(NDATA .EQ. NRDATA) GO TO 95
  338  PRINT 1005
  339  GO TO 200
  340  95  NEL=0

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342      NEWD=0
343      NEADY=0
344      IF (DMAX .GE. RMAX) NEWHGR=0
345      GO TO 10
346
C... F 104 EXIT'S
347      9008    PRINT 1008
348      GO TO 910
349      9009    PRINT 1009
350      GO TO 940
351      910     PRINT 1010
352      GO TO 940
353      911     PRINT 1011
354      GO TO 940
355      912     PRINT 1012
356      GO TO 940
357      913     PRINT 1013
358      GO TO 940
359      914     PRINT 1014
360      GO TO 940
361      915     PRINT 1015
362      GO TO 940
363      916     PRINT 1016
364      GO TO 940
365      917     PRINT 1017
366      GO TO 940
367      989     PRINT 998
C...CLOSE PLOT FILE
368
359      IF (NRCVS .GT. 0) CALL PLOT(0,0,999)
370      PRINT 1000,NRCVS,NRPLTS
371      STOP
C
372      998     FORMAT('0***** END OF DATA SET ON UNIT 5 *****')
373      999     FORMAT('1ADDITIONAL PLOT IDENTIFICATION: ', 'AB,1X,A8')
374      1000    FORMAT('0END OF JOB: ', '14, ' CURVES AND ', 14, ' GRAPHS GENERATED')
375
376      1001    FORMAT(20A4)
377      1002    FORMAT(1X,20A4)
378      1003    FORMAT(1X,20A4)
379      1004    FORMAT(1X,A2, ' COMPONENT1 OPTION ', 12)
380      1005    FORMAT(1X)
381      1006    FORMAT(5(  *  ), ' NRCURV GT 4' )
382      1007    FORMAT(5(  *  ), ' NUMBER OF MODES EQ 0' )
383      1010    FORMAT(5(  *  ), ' UNIDENTIFIED CONTROL CARD' )
384      1011    FORMAT(5(  *  ), ' INPUT RHO VALUES OUT OF ORDER' )
385      1012    FORMAT(5(  *  ), ' NO OPTION NUMBER 3' )
386      1013    FORMAT(5(  *  ), ' SIZEY CANNOT BE GT 8' )
387      1014    FORMAT(5(  *  ), ' NUMBER OF MODES REDUCED' )
388      1015    FORMAT(5(  *  ), ' INSUFFICIENT DATA FOR WKB MODE SUM' )
389      1016    FORMAT(5(  *  ), ' NO MODE DATA INPUT' )
390      1017    FORMAT(5(  *  ), ' DIST BEYOND ', F7.3, ' WILL BE IGNORED' )
391      1018    FORMAT(5(  *  ), ' NO USABLE DISTANCE DATA' )
392      1019    FORMAT(5(  *  ), ' ERROR IN DATA' )
393      1020    FORMAT(1X,F7.0,3(2X,FB0),2(2X,E10.0),2X,E5.0)
394      1021    FORMAT('0', F7.3, ' F', FB.4, ' A', FA.3, ' C', FB.3, ' M', F6.3,
395      $           ' S', '1PE10.3, ' E', '0PF5.1)
396      1022    FORMAT(11,2F9.0,1X,4E15.0)
397      1023    FORMAT(10X,12,3X,11,0P2F10.5,2(1X,1P2E16.8)/
398      $           15X, '11,0P2F10.5,2(1X,1P2E16.8))
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```
399      1028  FORMAT('+' ,66X, 'MODES',13)
400      1030  FORMAT('0 DIST  MEAN A      STD')
401      1031  FORMAT(1X,F6.3,2F10.3)
402      1220  FORMAT(11X, 'USING DATA FROM PREVIOUS RHO')
403      1221  FORMAT(11X, 'M 1D THETA')
404      END
```



```

57      REWIND 3
58      REWIND 4
59
60      C...TRANSMITTER DATA
61      READ(3) STP,TP,AV1,EX,SIGMA,EPSR,RHO,MODES,NOMODE
62      RHO1=RHO
63      IF(NEWD .EQ. 0 .AND. NEWHGT .EQ. 0) GO TO 10
64      C...TRANSMITTER HEIGHT GAINS
65      CALL HTGAIN(1,FREQ,SIGMA,EPSR,ALPHA,MODES,TP,TALT,HGT)
66      10     IF(NEWD .EQ. 0 .AND. NEWHGR .EQ. 0) GO TO 11
67      C...RECEIVER HEIGHT GAINS
68      CALL HTGAIN(1,FREQ,SIGMA,EPSR,ALPHA,MODES,TP,RALT,HGT)
69      WRITE(4) HG
70      GO TO 12
71      11     READ(4) HG
72      C
73      C...SET UP MODE CONSTANTS
74      12     DO 14 M=1,MODES
75      IF(NOMODE(M)) GO TO 14
76      SUMA(M)=0.0
77      AV1(M)=AV1(M)
78      HG1(M)=HG(RCOMP,M)
79      DO 13 TCOMP=1,3
80      EX1(TCOMP,M)=EX(TCOMP,RCOMP,M)
81      XMT(TCOMP,M)=CDABS(EX1(TCOMP,M))
82      X=EX1(TCOMP,M)
83      Y=EX1(TCOMP,M)*MI
84      XAT(TCOMP,M)=DATAN2(Y,X)
85      XAR(TCOMP,M)=XAT(TCOMP,M)
86      CONTINUE
87      13     IF(NEWP .EQ. 0 .OR. NPRINT .EQ. 0) GO TO 20
88      C
89      C...PRINT TABLE OF MODE CONSTANTS AT TRANSMITTER
90      PRINT 1040,RHO1
91      DO 16 M=1,MODES
92      IF(NOMODE(M)) GO TO 15
93      STPR=STP(M)
94      STPI=STP(M)*MI
95      ATTEN=ACONST*STPI
96      VOVERC=1.0/STPR
97      TMP1=TMP4*EX1(1,M)*HG1(1,M)*HG1(1,M)
98      X=TMP1
99      Y=TMP1*MI
100     AMP1=10.0*DLOG10(X*Y*Y)
101     ANG1=DATAN2(Y,X)
102     TMP2=TMP4*EX1(2,M)*HG1(2,M)*HG1(1,M)
103     X=TMP2
104     Y=TMP2*MI
105     AMP2=10.0*DLOG10(X*Y*Y)
106     ANG2=DATAN2(Y,X)
107     TMP3=TMP4*EX1(3,M)*HG1(3,M)*HG1(1,M)
108     X=TMP3
109     Y=TMP3*MI
110     AMP3=10.0*DLOG10(X*Y*Y)
111     ANG3=DATAN2(Y,X)
112     S(M)=0.0
113     LNO(1,M)=AMP1

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```

114 LMO(2,M) = AMP2
115 LMO(3,M) = AMP3
116 PRINT 1041,M,ATTEN,VOVERC,AMP1,ANG1,AMP2,ANG2,AMP3,ANG3,
117 ,AMP1,AMP2,AMP3
118 GO TO 16
119 15 PRINT 1041,M
120 16 CONTINUE
121 C...RECEIVER POINT DATA
122 READ(3) STP,1P,AV2,EX,SIGMA,EPSR,RHO,MODES,NOMODE
123 20 RH02=RHO
124 1F (NEWD .EQ. 0 .AND. NEWGR .EQ. 0) GO TO 21
125 CALL HIGAIN(1,FREQ,SIGMA,EPSR,ALPHA,MODES,TP,RALT,HG)
126 WRITE(4) HG
127 GO TO 22
128 21 READ(4) HG
129 22 DO 23 M=1,MODES
130 HG2(M)=HG1(RCOMP,M)
131 DO 23 TCOMP=1,3
132 EX2(TCOMP,M)=EX(TCOMP,RCOMP,M)
133 23 EX2(TCOMP,M)=EX(TCOMP,RCOMP,M)
134 CONTINUE
135 1F (NEWP .EQ. 0 .OR. NPRINT .EQ. 0) GO TO 25
136 C...PRINT TABLE OF MODE CONSTANTS AT RECEIVER
137 PRINT 1040,RHO2
138 DRHO=8.686D0*(RHO2-RHO1)
139 DO 24 M=1,MODES
140 1F (NOMODE(M)) GO TO 240
141 STPR=SP(M)
142 STP1=SP(M)*MI
143 ATTEN=ACNST*STPI
144 NOVERC=1.D0/STPR
145 TMP1=MP4*EX2(1,M)*HGT(1,M)*HG2(M)
146 TMP2=MP4*EX2(2,M)*HGT(2,M)*HG2(M)
147 X=TMP1
148 Y=TMP1*MI
149 AMP1=10.D0*DLOG10(X*X+Y*Y)
150 ANG1=DATAN2(Y,X)
151 TMP2=MP4*EX2(2,M)*HGT(2,M)*HG2(M)
152 X=TMP2
153 Y=TMP2*MI
154 AMP2=10.D0*DLOG10(X*X+Y*Y)
155 ANG2=DATAN2(Y,X)
156 TMP3=MP4*EX2(3,M)*HGT(3,M)*HG2(M)
157 X=TMP3
158 Y=TMP3*MI
159 AMP3=10.D0*DLOG10(X*X+Y*Y)
160 ANG3=DATAN2(Y,X)
161 DAV=AV(1,M)+AV2(1,M)
162 S(M)=S(M)+DRHO*DAV
163 C...RELATIVE EXCITATION FACTORS AT BEGINNING OF SEGMENT
164 REL1=.5D0*(LMO(1,M)+AMP1+S(M))
165 REL2=.5D0*(LMO(2,M)+AMP2+S(M))
166 REL3=.5D0*(LMO(3,M)+AMP3+S(M))
167 PRINT 1041,M,ATTEN,VOVERC,AMP1,ANG1,AMP2,ANG2,AMP3,ANG3,
168 ,REL1,REL2,REL3
169 GO TO 24
170

```

```

240 PRINT 1041,M
171
172 C...SET UP LINEAR INTERPOLATION ARRAYS
173
174 24 CONTINUE
175 DRHO=RH02-RH01
176 IF(DRHO .EQ. 0.0D0) GO TO 27
177 DO 260 M=1,MODES
178 IF(NOMODE(M)) GO TO 260
179 SAV(M)=(AV2(M)-AV1(M))/DRHO
180 SHG(M)=(HG2(M)-HG1(M))/DRHO
181 DO 28 TCOMP=1,3
182 SEx(TCOMP,M)=(EX2(TCOMP,M)-EX1(TCOMP,M))/DRHO
183 260 CONTINUE
184 IF(RHOSUM .EQ. DST) GO TO 99
185 GO TO 30
186 C
187 C...DUPLICATE RHO DATA, ABRUPT CHANGE IN PATH ASSUMED
188 27 DO 28 M=1,MODES
189 AV1(M)=AV2(M)
190 HG1(M)=HG2(M)
191 DO 28 TCOMP=1,3
192 EX1(TCOMP,M)=EX2(TCOMP,M)
193 28 CONTINUE
194 GO TO 20
195 C
196 29 IF(RHOSUM .EQ. DST) GO TO 40
197 RHOSUM=RHOINC
198 IF(RHOSUM .GT. DST) RHOSUM=DST
199 IF(RHOSUM .GT. RHOMAX) GO TO 31
200 IF(RHOSUM .GT. RH02) RHOSUM=RHO2
201 DRHO=RHOINC-RH01
202 DRHO2=DRHO1-.5D0*DRHO
203
204 C...LOOP OVER MODES AT RECEIVER
205 DO 34 M=1,MODES
206 IF(NOMODE(M)) GO TO 34
207 C...INTEGRAL OVER S
208
209 SUMA(M)=SUMA(M)+(AV1(M)+SAV(M)*DRHO2)*DRHO
210 C...LOOP OVER TRANSMITTED COMPONENTS - FOR PHASE CONTINUITY
211 DO 33 TCOMP=1,3
212 EX1(TCOMP,M)=EX1(TCOMP,M)+SEX(TCOMP,M)*DRHO1
213 PHI=XAR(TCOMP,M)
214 X=EXR(TCOMP,M)
215 Y=EXR(TCOMP,M)*M1
216 PHI2=DATAN2(Y,X)
217 IF(PHI2-PHI1 .LE. P1) GO TO 32
218 PHI2=PHI2-TWOP1
219 GO TO 33
220 IF(PHI1-PHI2 .LE. P1) GO TO 33
221 PHI2=PHI2+TWOP1
222 XAR(TCOMP,M)=PHI12
223 CONTINUE
224 RH00=RHOSUM
225 C
226 IF(RHOSUM .LT. DST) GO TO 50
227 C

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```

C... MODE PARAMETERS AT RECEIVER DISTANCE
228  STEMM=SUM0/DSQRT(ABS(DSIN(DST/6.366D0)))
229  DO 39 M=1, MODES
230  IF (INOMODE(M)) GO TO 39
231  HGR=HG1(M)+SHGM(M)*DRHO1
232  DO 38 TCOMP=1,3
233  XMR=CDABS(SXR(TCOMP,M))
234  EXM=DSQRT(XMT(TCOMP,M)*XMR)
235  EXA=.5D0*(XAT(TCOMP,M)+XAR(TCOMP,M))
236  EXR=(TCOMP,M)=EXM*DQMLX(DCOS(EXA),DSIN(EXA))*HGT(TCOMP,M)*HGR
237  39  CONTINUE
238  C
239  C... MODE SUMMATION
240  SUM=0.D0
241  DO 42 M=1, MODES
242  IF (INOMODE(M)) GO TO 42
243  SUM=0.D0
244  DO 41 TCOMP=1,3
245  SUM=SUM+EXR(TCOMP,M)*T(TCOMP)
246  SUM=SUM+CDEXP(SUMA(M)-RST*A(M))*SUME
247  CONTINUE.
248  42  CONTINUE.
249  C
250  C... STORE MODE SUN PARAMETERS
251  SUM=SUM+STERM
252  SUMN=SUM
253  X=SUM
254  Y=SUM*M1
255  AMP=10.D0*DLOG10(X*X+Y*Y)
256  PHS=DATAN2(Y,X)*RTD
257  IF (PHS-PHZ .LE. 180.) GO TO 43
258  REV=REV-360.
259  GO TO 44
260  IF (PHZ-PHS .LE. 180.) GO TO 44
261  REV=REV+360.
262  PHZ=PHS
263  PHS=PHS+REV
264  IF (RHOSUM .EQ. RHO2 .AND. RHO2 .NE. RHOMAX) GO TO 51
265  GO TO 99
266  C
267  50  IF (RHOSUM .LT. RHO2 .OR. RHO2 .EQ. RHOMAX) GO TO 30
268  51  RHO1=RHO2
269  C... GO TO REASSIGN MODE CONSTANTS
270  GO TO 27
271  C
272  99  RSUM=RHOSUM
273  RETURN
274
275  1040  FORMAT('ORHO = ',F6.3,' MODE ATTN V/C',SX,'VERTICAL',9X,
276  9  'BROADSIDE',8X,'END FIRE',11X,'V',10X,'B',10X,'E')
277  1041  FORMAT(15X,13,F8.3,F9.5,(F10.3,F7.3),(4X,F7.2))
278  END

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```

1  SUBROUTINE POUT1(JJJ,JUMAX)
2  COMMON/DIMEN/SIZEX,SIZEY,AMPMAX,AMPMIN,AMPIINC,PHSMAX,
3  PHSMIN,PHSINC,XMAX,XMIN,XINC,SKIP1(3),
4  NRCURV,NAPLOT,NPPLOT,NPDIFF,NPRINT
5  COMMON/IDENT/ID120,FREQ,TALT,RALT,ICOMP,ZYX,IOPT,THET,INCL,
6  DST,RADIUS,POWER
7  COMMON/OUTPUT/XY(501),OUT1(501),OUT2(501),NRPTS,NRCRVS,
8  NRPLTS,DT(4)
9  COMMON PHI1(501),UP(501),XL(2),YL(2),UL(2)
10 LOGICAL UP,UL
11 REAL INCL
12 C
13  IR=-1
14  KK=MOD(JJJ,NRCURV)
15  IF(KK .EQ. 0) KK=NRCURV
16  IF(JJJ .GT. 1) GO TO 10
17  NFRAME=1
18  OFFSET=AMAX1(10,5,SIZEX+2,5)
19  DO 1 I=1,NRPTS
20  PHI1(I)=OUT2(I)
21  C
22  10 IF(NPRINT .EQ. 0) GO TO 20
23  PRINT 1001,ZYX,INCL,THET,TALT,RALT
24  NL=NRPTS/4+1
25  DD 19 I=1,NL
26  PRINT 1011,(XY(I),OUT1(I),OUT2(I)),I=11,NRPTS,NL)
27  C
28  20 IF(NAPLOT .EQ. 0) GO TO 30
29  IR=IR+1
30  NPLOT=1
31  AMAX=AMPMAX
32  AMIN=AMPMIN
33  AINC=AMPIINC
34  DO 29 I=1,NRPTS
35  UP(I)=.FALSE.
36  IF(OUT1(I) .LE. AMAX) GO TO 27
37  OUT1(I)=AMAX
38  GO TO 28
39  27 IF(OUT1(I) .GE. AMIN) GO TO 29
40  OUT1(I)=AMIN
41  28 UP(I)=.TRUE.
42  CONTINUE.
43  YMAX=AMAX
44  YMIN=AMIN
45  YINC=AINC
46  GO TO 100
47  C
48  30 IF(NPLOT .EQ. 0) GO TO 40
49  IR=IR+1
50  IF(IR .NE. 0) CALL PLOT(OFFSET,0.,-3)
51  NPLT=2
52  FK=0.
53  DO 39 I=1,NRPTS
54  OUT1(I)=OUT2(I)+FK
55  UP(I)=.FALSE.
56  IF(OUT1(I) .LT. PHSMIN) GO TO 36

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57      IF(OUT1(I) .GT. PHSMAX) GO TO 37
58      GO TO 39
59      FK=FK-PHSMIN
60      OUT1(I)=OUT1(I)-PHSMIN
61      GO TO 38
62      FK=FK-PHSMAX
63      OUT1(I)=OUT1(I)-PHSMAX
64      UP(I)=.TRUE.
65      GO TO 35
66      CONTINUE
67      YMAX=PHSMAX
68      YMIN=PHSMIN
69      YINC=PHSINC
70      GO TO 100
71      C
72      40      IF(NPDIFF .EQ. 0) GO TO 50
73      IR=IR+1
74      IF(IR .NE. 0) CALL PLOT(OFFSET,0.,-3)
75      NPLT=3
76      FK=0.
77      DO 49 I=1,NRPTS
78      OUT1(I)=OUT2(I)-FH1(I)+FK
79      UP(I)=.FALSE.
80      45      IF(OUT1(I) .LT. PHSMIN) GO TO 46
81      IF(OUT1(I) .GT. PHSMAX) GO TO 47
82      GO TO 49
83      46      FK=FK-PHSMIN
84      OUT1(I)=OUT1(I)-PHSMIN
85      GO TO 48
86      FK=FK-PHSMAX
87      OUT1(I)=OUT1(I)-PHSMAX
88      UP(I)=.TRUE.
89      GO TO 45
90      CONTINUE
91      YMAX=PHSMAX
92      YMIN=PHSMIN
93      YINC=PHSINC
94      GO TO 100
95      C
96      50      IF(MM .EQ. NRCURV .OR. JU .EQ. JUMAX) GO TO 51
97      IF(IR .EQ. 0) GO TO 99
98      CALL PLOT(-1R*OFFSET1,0.,-3)
99      GO TO 99
100     51      CALL PLOT(0.,0.,-4)
101     NFRAME=1
102     99      RETURN
103     C
104     100     IF(MM .NE. 1) GO TO 130
105     IF(NFRAME .EQ. 1) CALL PLOT(1.5,2.0,-3)
106     NFRAME=0
107     NRPLTS=NRPLTS+1
108     XP=0.
109     YP=-.4
110     CALL SYMBOL(XP,YP,.1,4HFLD4,0.,4)
111     XP=XP+.5
112     CALL NUMBER(XP,YP,.1,FLOAT(NRPLTS),0.,-1)
113     XP=XP+.0

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114 CALL SYMBOL(XP,YP,.1,0T,0..16)
115 XP=0.
116 YP=YP-.15
117 IF(NPLDT-2) 101,102,103
118 CALL SYMBOL(XP,YP,.1,9AMPLITUDE,0..9)
119 GO TO 104
120 CALL SYMBOL(XP,YP,.1,14HRELATIVE PHASE,0..14)
121 GO TO 104
122 103 CALL SYMBOL(XP,YP,.1,12HPHASE-PHASE1,0..12)
123 XP=0.
124 YP=YP-.15
125 CALL SYMBOL(XP,YP,.1,2YX,0..1)
126 XP=XP+0.2
127 CALL S790L(XP,YP,.1,9HCOMPONENT,0..9)
128 XP=XP+1.5
129 CALL SYMBOL(XP,YP,.1,6HFREQ =,0..6)
130 XP=XP+0.7
131 CALL NUMBER(XP,YP,.1,FREQ,0..3)
132 XP=XP+1.0
133 CALL SYMBOL(XP,YP,.1,7HPOWER =,0..7)
134 XP=XP+0.8
135 CALL NUMBER(XP,YP,.1,POWER,0..1)
136 XP=0.
137 YP=YP-.15
138 CALL SYMBOL(XP,YP,.1,6HTALT =,0..6)
139 XP=XP+0.7
140 CALL NUMBER(XP,YP,.1,TALT,0..1)
141 XP=XP+1.0
142 CALL SYMBOL(XP,YP,.1,6HRLALT =,0..6)
143 XP=XP+0.7
144 CALL NUMBER(XP,YP,.1,RALT,0..1)
145 XP=XP+1.0
146 IF(LOPT .EQ. 1) GO TO 118
147 XP=0.
148 YP=YP-.15
149 CALL SYMBOL(XP,YP,.1,6HINCL =,0..6)
150 XP=XP+0.7
151 CALL NUMBER(XP,YP,.1,INCL,0..3)
152 XP=XP+1.0
153 CALL SYMBOL(XP,YP,.1,7HTHETA =,0..7)
154 XP=XP+0.8
155 CALL NUMBER(XP,YP,.1, 'ET,0..3)
156 XP=XP+1.0
157 GO TO 119
158 XP=0.
159 YP=YP-.15
160 CALL SYMBOL(XP,YP,.1,1D,0..80)
161 CALL BORDER(SIZEX,XMIN,XMAX,XINC,1,SIZEY,YMIN,YMAX,YINC,1)
162 YP0=YP
163 NRCVS=NRCVS+1
164 XP=0.
165 YP=YP0-.15*KK
166 XL(1)=-1.1
167 XL(2)=-0.1
168 YL(1)=YP
169 YL(2)=YP
170

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1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56
      SUBROUTINE POUT2(JJ,II)
      COMMON/IDENT/ID(20),FREQ,TALT,RALT,ICONMP,2YX,IOPT,THTANG,INCANG,
      DIST,RADIUS,POWER
      COMMON/DIMEN/SIZEX,SKIP2(10),TMAX,TMIN,SKIP3(5),NPRINT
      COMMON/OUTPUT/T(501),AMP(501),PHS(501),NRPPTS,NRCRV5,NRPPTS,DT(4)
      COMMON UP(501)
      LOGICAL UP
      CHARACTER 2YX
      REAL INCANG
      C
      IF(II .GT. 1 .OR. JJ .GT. 1) GO TO 9
      NRPLTS=NRPLTS+1
      YP=9.8
      CALL SYMBOL(0.0,YP,.1,4HFLD4,0.,4)
      CALL NUMBER(0.5,YP,.1,FLOAT(NRPLTS),0.,-1)
      CALL SYMBOL(1.0,YP,.1,DT,0.,16)
      YP=YP-.2
      CALL SYMBOL(0.0,YP,.1,1D,0.,80)
      YP=YP-.2
      CALL SYMBOL(0.0,YP,.1,ZYX,0.,1)
      CALL SYMBOL(0.2,YP,.1,9HCOMPONENT,0.,9)
      YP=YP-.2
      CALL SYMBOL(0.0,YP,.1,23HFREQ, " )
      CALL NUMBER(0.7,YP,.1,FREQ,0.,3)
      CALL NUMBER(2.3,YP,.1,POWER,0.,1)
      YP=YP-.2
      CALL SYMBOL(0.0,YP,.1,23HT, ALT, " )
      CALL NUMBER(0.8,YP,.1,TALT,0.,1)
      CALL NUMBER(2.3,YP,.1,RALT,0.,1)
      YP=YP-.2
      CALL SYMBOL(0.0,YP,.1,7HINCL, " )
      CALL NUMBER(0.7,YP,.1,INCANG,0.,3)
      YP=YP-.2
      CALL SYMBOL(0.0,YP,.1,9HRADIUS, " )
      CALL NUMBER(0.9,YP,.1,RADIUS,0.,4)
      YP=YP-.2
      C
      IF(JJ .GT. 1) GO TO 33
      C
      IF(NPRINT .EQ. 0) GO TO 20
      PRINT 1000,2YX,DIST,INCANG
      NL=NRPTS/4+1
      DO 19 I=1,NL
      PRINT 1011,(T(I),AMP(I),PHS(I),I=I1,NRPTS,NL)
      C
      CALL SYMBOL(0.00,-.40,.10,7HDIST, " )
      CALL NUMBER(0.70,-.40,.10,DIST,0.,3)
      CALL BORDER(SIZEX,TMIN,TMAX,90,14,-360.,360.,90.,1)
      CALL SYMBOL(-.2,1.7,.1,7HDEGREES,90.,7)
      C
      NRCRV5=NRCRV5+1
      FK=0
      DO 38 J=1,NRPTS
      YP=PHS(J)+FK
      UP(J)=.FALSE.
      IF(YP .LT. -360.) GO TO 35

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57      IF(YP .GT. 360.) GO TO 36
58      GO TO 38
59      FK=FK+360.
60      YP=YP+360.
61      GO TO 37
62      FK=FK-360.
63      YP=YP-360.
64      UP(J)=.TRUE.
65      GO TO 34
66      PHS(J)=YP
67      CALL CURVE(T,PHS,UP,NRPTS,TMIN,-360.,(TMAX-TMIN)/SIZEX,100.,JJ)
68
C      NRCRVS=NRCRVS+1
69      CALL PLOT(0.,4.3,-3)
70      1F(JJ,GT,1) GO TO 44
71      AMAX=-100.
72      AMIN= 100.
73      DO 40 J=1,NRPTS
74      AMPJ=AMP(J)
75      IF(AMIN .GT. AMPJ) AMIN=AMPJ
76      IF(AMIN .LT. AMPJ) AMAX=AMPJ
77      IF(AMAX .LT. AMPJ) AMAX=AMPJ
78      CONTINUE
79      AMIN=AMIN-40.
80      CALL BORDER(SIZEX,TMIN,TMAX,90.,14.,AMIN,AMAX,10.,10.)
81      CALL SYMBOL(-2,1.5,.1,10HDB/UV/N,KW,90.,10)
82      DO 48 J=1,NRPTS
83      AMPJ=AMP(J)
84      AMPJ=AMP(J)
85      UP(J)=.FALSE.
86      IF(AMPJ .LE. AMAX) GO TO 46
87      AMPJ=AMAX
88      GO TO 47
89      46      IF(AMPJ .GE. AMIN) GO TO 48
90      AMPJ=AMIN
91      47      UP(J)=.TRUE.
92      48      AMP(J)=AMPJ
93      CALL CURVE(T,AMP,UP,NRPTS,TMIN,AMIN,(TMAX-TMIN)/SIZEX,10.,JJ)
94
C      CALL PLOT(0.,-4.3,-3)
95
96      99      RETURN
97      1000  FORMAT('0',A1,'COMP DIST = ',F7.3,' INCL = ',F7.3/
98      98      $ 4('THETA AMPLITUDE PHASE',7X))
99      1011  FORMAT(4(F7.3,2F10.4,5X))
100
END

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1      SUBROUTINE CURVE(X,Y,UP,NRPTS,XMIN,YMIN,XINC,YINC,LINE)
2
3      C X,Y,UP MUST BE DIMENSIONED AT LEAST NRPTS
4      C XMIN,YMIN ARE X,Y ORIGIN IN USER UNITS
5      C XINC,YINC ARE X,Y SCALES IN USER UNITS PER INCH
6
7      C LINE=1:  SOLID
8      C   2:  LONG DASH
9      C   3:  MEDIUM DASH
10     C   4:  SHORT DASH
11     C   5:  DOTTED
12     C   6:  SHORT + LONG DASH
13     C   7:  SHORT + SHORT + LONG DASH
14
15      LOGICAL UP,UP1,UP2
16      DIMENSION IPEN(10),JDC(7),X(NRPTS),Y(NRPTS),UP(NRPTS),
17      DATA IPEN/3,2,3,2,2,2,2/,JDC/18,61,56,52,11,36/
18      DATA DELR/.1/
19
20      IF(NRPTS.LE.1) GO TO 99
21
22      IF(LINE) 1,2,3
23      1  KK=MOD(LINE,7)+7
24      2  GO TO 4
25      2  KK=0
26      2  GO TO 4
27      3  KK=MOD(LINE,7)
28      4  KK=KK+1
29      4  JO=JDC(KK)/10
30      4  JC=JDC(KK)-10*JO
31
32      J=1
33      IP=2
34      IF(KK .EQ. 6) IP=3
35      DR=0.
36      RHO1=0.
37      RHO2=DELR
38      PX1=(X(1)-XMIN)/XINC
39      PY1=(Y(1)-YMIN)/YINC
40      UP1=UP(1)
41      IF(UP1) GO TO 10
42
43      C GO TO FIRST POSITION WITH PEN UP
44      CALL PLOT(PX1,PY1,3)
45
46      DO 40 I=2,NRPTS
47      PX2=(X(I)-XMIN)/XINC
48      PY2=(Y(I)-YMIN)/YINC
49      UP2=UP(I)
50      IF(UP2) GO TO 22
51      IF(UP1) GO TO 37
52      IF(KK .EQ. 2) GO TO 38
53      DELX=PX2-PX1
54      DELY=PY2-PY1
55      RHO2=SQRT(DELX**2+DELY**2)
56
57      RHO1=RHO1+RHO2
58
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57      IF(RHO2 .GT. RHO1) GO TO 38
58      DELX=DELX*DELR/RHO
59      DELY=DELY*DELR/RHO
60      DX 6=DELX*.1
61      DY 6=DELY*.1
62      IF(DR .EQ. 0.) GO TO 20
63      DX=DELX*DR/DELR
64      DY=DELY*DR/DELR
65      PX1=PX1+DX
66      PY1=PY1+DY
67      GO TO 21
68      IF(RHO2 .GT. RHO1) GO TO 38
69      PX1=PX1+DELX
70      PY1=PY1+DELY
71      CALL PLOT(PX1, PY1, 1P)
72      IF(KK .EQ. 6) CALL PLOT(PX1+DX6, PY1+DY6, 2)
73      J=J+1
74      IP=IPEN(J0+MOD(J,JC))
75      RHO2=RHO2+DELR
76      GO TO 20
77      DR=0.
78      RHO1=0.
79      RHO2=DELR
80      GO TO 39
81      C PEN HAS BEEN UP, PREPARE TO LOWER PEN
82      CALL PLOT(PX2, PY2, 3)
83      GO TO 39
84      CALL PLOT(PX2, PY2, 1P)
85      DR=RHO2-RHO1
86      PX1=PX2
87      PY1=PY2
88      UP1=UP2
89      CONTINUE
90      RETURN
91      END

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1      SUBROUTINE BORDER(XLNG,XMIN,XMAX,XINC,NX,YLNG,YMIN,YMAX,YINC,NY)
2      DIMENSION XINC(NX),YINC(NY)
3      LOGICAL FY,FX
4      FX=.FALSE.
5      FY=.FALSE.
6      IF(NX .EQ. 1) FX=.TRUE.
7      IF(NY .EQ. 1) FY=.TRUE.
8      XT=XINC(1)
9      YT=YLNG(1)
10     XSCALE=XLNG/(XMAX-XMIN)
11     YSCALE=YLNG/(YMAX-YMIN)
12     YM=ABS(YMIN)
13     YLN=-.4
14     IF(YM .GE. 10.) YLN=YLN-.1
15     IF(YM .GE. 100.) YLN=YLN-.1
16     IF(YM .GE. 1000.) YLN=YLN-.1
17     IF(YMIN .LT. 0.) YLN=YLN-.1
18     YM=ABS(YMAX)
19     YLM=-.4
20     IF(YM .GE. 10.) YLM=YLM-.1
21     IF(YM .GE. 100.) YLM=YLM-.1
22     IF(YM .GE. 1000.) YLM=YLM-.1
23     IF(YMAX .LT. 0.) YLM=YLM-.1
24     XM=ABS(XMAX)
25     XLM=-.3
26     IF(XM .GE. 10.) XLM=XLM-.1
27     IF(XM .GE. 100.) XLM=XLM-.1
28     IF(XM .GE. 1000.) XLM=XLM-.1
29     IF(XMAX .LT. 0.) XLM=XLM-.1
30     IF(FX) DX=XINC(1)
31     IF(FY) DY=YINC(1)
32     1Y*1
33     YL=0.
34     CALL NUMBER(YLN,0.,1,YMIN,0.,1)
35     CALL PLOT(0.,0.,3)
36     IF(FY) GO TO 110
37     10      YP=(YINC(1Y)-YMIN)*YSCALE
38     GO TO 111
39     110     YL=YL+DY
40     YP=YL*YSCALE
41     111     IF(YP .LT. 0.) GO TO 99
42     IF(YP .GE. YLNG) GO TO 11
43     CALL PLOT(0.,YP,2)
44     CALL PLOT(.1,YP,2)
45     CALL PLOT(0.,YP,2)
46     IF(FY) GO TO 110
47     1Y=1Y+1
48     IF(1Y .LE. NY) GO TO 10
49     CALL PLOT(0.,YLNG,2)
50     CALL NUMBER(YLM,YLNG-.1,.1,YMAX,0.,1)
51     CALL PLOT(0.,YLNG,3)
52     1X*1
53     XL=0.
54     IF(FX) GO TO 112
55     XP=(XINC(1X)-XMIN)*XSCALE
56     GO TO 120

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57      112      X1=X1+DX
58      120      XP=X1-XSCALE
59      120      IF (XP .LT. 0.) GO TO 99
60      120      IF (XP .GE. XLNG) GO TO 13
61      120      CALL PLOT(XP,YLNG,2)
62      120      CALL PLOT(XP,YT,2)
63      120      CALL PLOT(XP,YLNG,2)
64      120      IF (FX) GO TO 112
65      120      IX=IX+1
66      120      IF (IX .LE. NX) GO TO 12
67      120      CALL PLOT(XLNG,YLNG,2)
68      120      IF (FY) GO TO 130
69      113      IY=IY-1
70      113      IF (IY .LE. 0) GO TO 15
71      113      YP=(YINC(IY)-YMIN)*YSCALE
72      113      GO TO 14
73      130      YL=YL-DY
74      130      YP=Y*YSCALE
75      140      IF (YP .LE. 0.) GO TO 15
76      140      CALL PLOT(XLNG,YP,2)
77      140      CALL PLOT(XT,YP,2)
78      140      CALL PLOT(XLNG,YP,2)
79      140      IF (FY) GO TO 130
80      140      GO TO 113
81      150      CALL PLOT(XLNG,0.,2)
82      150      CALL NUMBER(XLNG+XLIN,-.2,.1,XMAX,0.,1)
83      150      CALL PLOT(XLNG,0.,3)
84      150      IF (FX) GO TO 150
85      115      IX=IX-1
86      115      IF (IX .LE. 0) GO TO 17
87      115      XP=(XINC(IX)-XMIN)*XSCALE
88      150      GO TO 16
89      150      XL=XL-DX
90      150      XP=XL*XSCALE
91      160      IF (XP .LE. 0.) GO TO 17
92      160      CALL PLOT(XP,0.,2)
93      160      CALL PLOT(XP,1.,2)
94      160      CALL PLOT(XP,0.,2)
95      160      IF (FX) GO TO 150
96      160      GO TO 115
97      170      CALL PLOT(0.,0.,2)
98      170      CALL NUMBER(0.,-.2,.1,XMIN,0.,1)
99      99       RETURN
100     99       PRINT 100,XLNG,XMIN,XMAX,XINC(1),NX,YLNG,YMIN,YMAX,YINC(1),NY
101     100      FORMAT(0***,ERROR IN BORDER: XLNG, XMIN, XMAX, XINC(1), NX = '
102     100      $ 1P4E15.5,15/24X,YLNG, YMIN, YMAX, YINC(1), NY = ',1P4E15.5,BORDER0
103     103      $ 15/'0***')
104     104      CALL PLOT(0.,0.,999)
105     105      STOP
106     106      END

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1      SUBROUTINE HTGAIN(IOPT,FREQ,SIGMA,EPSR,ALPHA,NRMODE,TP,Z,HG)
2      IMPLICIT REAL*8 (A-H,O-Z)
3      COMPLEX*16 TP(1),HG(3,1),HG0/(0.0,1.45749544D0)/,
4      S,C,SSQ,CSQ,NGSQ,SQROOT,RATIO,A1,A2,A3,A4,
5      P0,H10,H20,H1PRMO,PZ,H1Z,H2Z,H1PRMZ,H2PRMZ,EXPZ,HTGAIN00
6      1/(0.0,1.00)/,M1/(0.0,-1.00)/,ONE/(1.00,0.00)/
7      REAL*8 K,KA13,KA23
8      DATA DTR/1.745329252D-02/
9
10      OMEGA=6.2831853072D03*FREQ
11      NGSO=DCMPLX(EPSR,-SIGMA/(8.85434D-12*OMEGA))
12      K=2.095E-026D-02*FREQ
13      IF (ALPHA .EQ. 0.0D0) GO TO 5
14      AK=ALPHA/K
15      AK13=DEXPDLOG(AK)/3.0D0
16      AK23=AK13**2
17      KA13=1.0D0/AK13
18      KA23=KA13**2
19      P1=KA23*ALPHA*Z
20      EXPZ=DEXP(-SD0*ALPHA*Z)
21      DO 20 M=.NRMODE
22      S=CDSIN(TP(M)*DTR)
23      SSQ=S*S
24      CSQ=ONE-SSQ
25      SQROOT=CSQRT(NGSQ-SSQ)
26      TEST=TP(M)*I
27      IF (TEST .GT. 10.0D0 .OR. ALPHA .EQ. 0.0D0) GO TO 10
28      PO=KA23*CSQ
29      CALL MDHNKL(P0,H10,H20,H1PRMO,H2PRMO,TP(M),'HG 1')
30      PZ=P0+P1
31      CALL MDHNKL(PZ,H1Z,H2Z,H1PRMZ,H2PRMZ,TP(M),'HG 2')
32      A1=H10 *H2Z -H1Z *H20
33      A2=H1PRMO*H2Z -H1Z *H2PRMO
34      A3=H10 *H2PRMZ-H1PRMZ**H20
35      A4=H1PRMO-H2PRMZ-H1PRMZ+H2PRMO
36      RATIO=SQROOT/NGSQ
37      C=.5D0+AK23+KA13*M1*RATIO
38      HG(1,M)=EXPZ*(C*A1+A2)
39      HG(2,M)=MA13*M1*SQROOT*A1+A2
40      HG(3,M)=.5D0*AK*M1*HG(1,M)+AK13*M1*EXPZ*(C*A3+A4)
41      IF (IOPT .EQ. 1) GO TO 20
42      HG(1,M)=HG(1,M)/HG0
43      HG(2,M)=HG(2,M)/HG0
44      HG(3,M)=HG(3,M)/(RATIO*HG0)
45      GO TO 20
46      C=CDSORT(CSQ)
47      EXPZ=CDEXP(DCMPLX(0.0D0,K*Z)*C)
48      A1=(NGSQ*C-SQROOT)/(NGSQ*C+SQROOT)
49      A2=(C-SQROOT)/(C+SQROOT)
50      HG(1,M)=EXPZ+A1/EXPZ
51      HG(2,M)=EXPZ+A2/EXPZ
52      HG(3,M)=(EXPZ-A1/EXPZ)*C
53      IF (IOPT .EQ. 1) GO TO 20
54      HG(1,M)=HG(1,M)/(ONE+A1)
55      HG(2,M)=HG(2,M)/(ONE+A2)
56      HG(3,M)=HG(3,M)/(ONE+A1)*C

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20 CONTINUE
 RETURN
 END

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1 SUBROUTINE MDHNKL (Z,H1,H2,H1PRME,H2PRME,THETA, IDBG)
2 IMPLICIT COMPLEX*16 (A-H,D-Z)
3 COMPLEX*16 I,MI,MPWNR,MTERM
4 REAL*8 A,B,C,D,CAP,PART1,PART2,ZMAC
5 DIMENSION A(30), B(30), C(30), D(30), CAP(30), PART1(2), PART2(2)
6 EQUIVALENCE (PART1,TERM4). (PART2,SUM4)
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11 5.4168543740434216542D-02,
12 9.345849566311674231D-01,
13 6.121004300561072794D-00,
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15 2.8842080097260218300D-03,
16 2.5827494893312753646D-05,
17 1.415573656074870734D-07,
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20 1.9948392989517716386D-15,
21 2.393809525516785112D-18,
22 2.1149208514407528762D-21,
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27 1.0785312873841039006D-01,
28 6.1360372635097223595D-01,
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30 2.3316778764072130571D-04,
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60      6.0764877832340288572D-01,    8.42202489582853564D-02, MDHNKLOO
61      1.002621486855016149D-02,    1.0363912784032058021D-03, MDHNKLOO
62      9.3867869420580435442D-05,    7.5124342D-06, MDHNKLOO
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67      1.0228117913786334592D-17,    3.19574823459247792364D-19, MDHNKLOO
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76      1.8370737967633072978D+08,    2.0679040329451551508D+09, MDHNKLOO
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78      4.277112686513471582D+12,    6.0971132411392560745D+13, MDHNKLOO
79      9.1486942234356367692D+14,    1.441352517000935010D+16, MDHNKLOO
80      2.3788844395175757942D+17,    4.104608160946921885D+18, MDHNKLOO
81      7.3900049415704853993D+19,    1.385922000460394314D+21, MDHNKLOO
82      2.7030825930275761623D+22,    5.4747478619645573335D+23, MDHNKLOO
83      1.1498937014386333524D+25,    2.5014180692753603969D+26, MDHNKLOO
84      DATA I/(0.00,1.00)/,MI/(0.00,-1.00)/, MDHNKLOO
85      DATA ONE/(1.00,0.0D)/,TWO/(2.00,0.0D)/,ZERO/(0.00,0.0D)/, MDHNKLOO
86      DATA ROOT3/(1.7320507568800,0.0D)/, MDHNKLOO
87      DATA ALPHA/(8.53667218B38951D-1,0.0D)/, MDHNKLOO
88      DATA CONST1/(-2.5881904510522D-01,-9.65925826289067D-01)/, MDHNKLOO
89      DATA CONST2/(2.5881904510522D-01,9.65925826289067D-01)/, MDHNKLOO
90      DATA CONST3/(-9.65925826289067D-01,2.58819045102522D-01)/, MDHNKLOO
91      DATA CONST4/(-9.65925826289067D-01,-2.58819045102522D-01)/, MDHNKLOO
92      C
93      ZPOWER=ONE
94      SUM3=ZERO
95      SUM4=ZERO
96      ZMAG=CDABS(Z)
97      IF(ZMAG.GT. 6.1D0) GO TO 70
98      SUM1=ZERO
99      SUM2=ZERO
100     ZTERM=-Z**3/(200.0D,0.0D)
101     DO 50 M=1,30
102     SUM1=SUM1+DCMPLX(A(M),0.0D)*ZPOWER
103     SUM2=SUM2+DCMPLX(B(M),0.0D)*ZPOWER
104     SUM3=SUM3+DCMPLX(C(M),0.0D)*ZPOWER
105     TERM4=DCMPLX(D(M),0.0D)*ZPOWER
106     SUM4=SUM4+TERM4
107     IF(DABS(PART1(1)/PART2(1)) .LE. 1.D-17 .AND.
108     Z DABS(PART1(2)/PART2(2)) .LE. 1.D-17) GO TO 60
109     50
110     CONTINUE
111     60
112     GM2F=1.0*(Z*SUM2-TWO*SUM1)/ROOT3
113     H1=Z*SUM2+GM2F

```

```

H2+H1-TWO*GM2F
H1PRME=SUM4+GPMFP
H2PRME=H1PRME-TWO*GPMFP
GO TO 999

      C      70      MPOWER=ONE
      114      SUM1=ONE
      115      SUM2=ONE
      116      RTZ=CDQRT(Z)
      117      SQRZ2=RTZ*Z
      118      2*TERM1=SQRZ2
      119      MTERM=ZTERM
      120      DM=ZERO
      121      TERM3=ONE
      122      DO 80 M=1,30
      123      ZPOWER=ZPOWER*ZTERM
      124      MPOWER=MPOWER*MTERM
      125      DM=DM+ONE
      126      TERM1=DCMPLX(CAP(M),0.0)*ZPOWER
      127      TERM2=DCMPLX(CAP(M),0.0)*MPOWER
      128      IF(CDABS(TERM2/TERM3)>.001) GO TO 81
      129      SUM1=SUM1+TERM1
      130      SUM2=SUM2+TERM2
      131      SUM3=SUM3+DM*TERM1
      132      TERM4=DM*TERM2
      133      SUM4=SUM4+TERM4
      134      IF(DABS(PART1(1)/PART2(1))>1.0-17) AND.
      135      $      DABS(PART1(2)/PART2(2))>1.0-17) GO TO 81
      136      TERM3=TERM2
      137      CONTINUE
      138      80      ZTERM=(1.5D0,0.00)/Z
      139      81      SUM3=SUM3+ZTERM
      140      SUM4=SUM4+ZTERM
      141      TERM1=(-0.25D0,0.00)-1*(SQRZ2)/Z
      142      TERM2=(-0.25D0,0.00)+1*(SQRZ2)/Z
      143      EXP=COEXP((0.00,0.66666666666666667D0)*SQRZ2B)
      144      EXP2=CONST1*EXP1
      145      EXP3=CONST2*EXP1
      146      EXP4=CONST3*EXP1
      147      EXP5=CONST4*EXP1
      148      ZTERM=ALPHA/CDSQRT(RTZ)
      149      TERM4=ZTERM*EXP2*SUM2
      150      TERM5=(PART1(1)-GE.0.D0.OR. PART1(2).GE.0.D0) GO TO 90
      151      H1=ZTERM*(EXP2*SUM2+EXP5*SUM1)
      152      H1PRME=ZTERM*(EXP2*(SUM2*TERM2+SUM4)+EXP5*(SUM1*TERM1+SUM3)))
      153      GO TO 110
      154      90      H1=ZTERM*EXP2*SUM2
      155      H1PRME=ZTERM*EXP2*(SUM2*TERM2+SUM4)
      156      110      IF(PART1(1).GE.0.D0.OR. PART1(2).LT.0.D0) GO TO 120
      157      H2=ZTERM*(EXP3*SUM1+EXP4*SUM2)
      158      H2PRME=ZTERM*(EXP3*(SUM1*TERM1+SUM3)+EXP4*(SUM2*TERM2+SUM4)))
      159      GO TO 999
      160      120      H2=ZTERM*EXP3*SUM1
      161      H2PRME=ZTERM*EXP3*(SUM1*TERM1+SUM3)
      162      167      CALCULATE WRONSKIAN AS PARTIAL CHECK ON VALIDITY
      163      168      SUM4=H1*H2PRME-H1PRME*H2
      164      999

```

```
171 IF(DABS(PART2(1)) .LE. 1.D-8 .AND.  
172  S DABS(PART2(2))+1.457495441040461D0) .LE. 1.D-8) GO TO 1000  
173  PRINT 1001,SUM4,THETA,IDBG  
174 1000 RETURN  
175 1001 FORMAT(1 **** POSSIBLE ERROR IN MDHNKL: W = ',1P2E15.6,  
176  S FOR THETA = ',0P2F10.4, AT ',A4)  
177 END  
MDHNKL00  
MDHNKL00  
MDHNKL00  
MDHNKL00  
MDHNKL00  
MDHNKL00  
MDHNKL00  
MDHNKL00
```

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